

Azimuthally-sensitive pion HBT in STAR

**Christopher Anson
for the STAR collaboration**

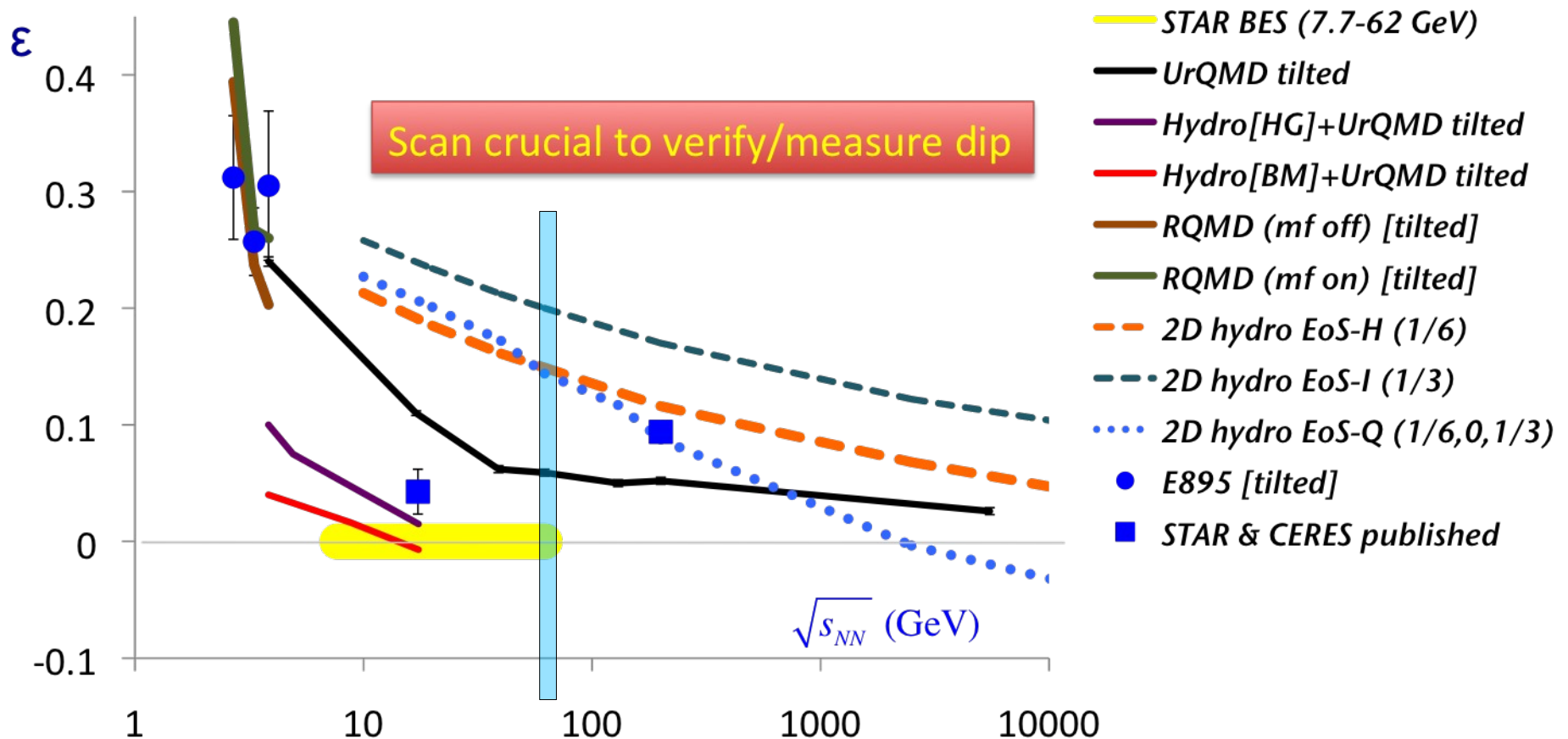
Ohio State University

Outline

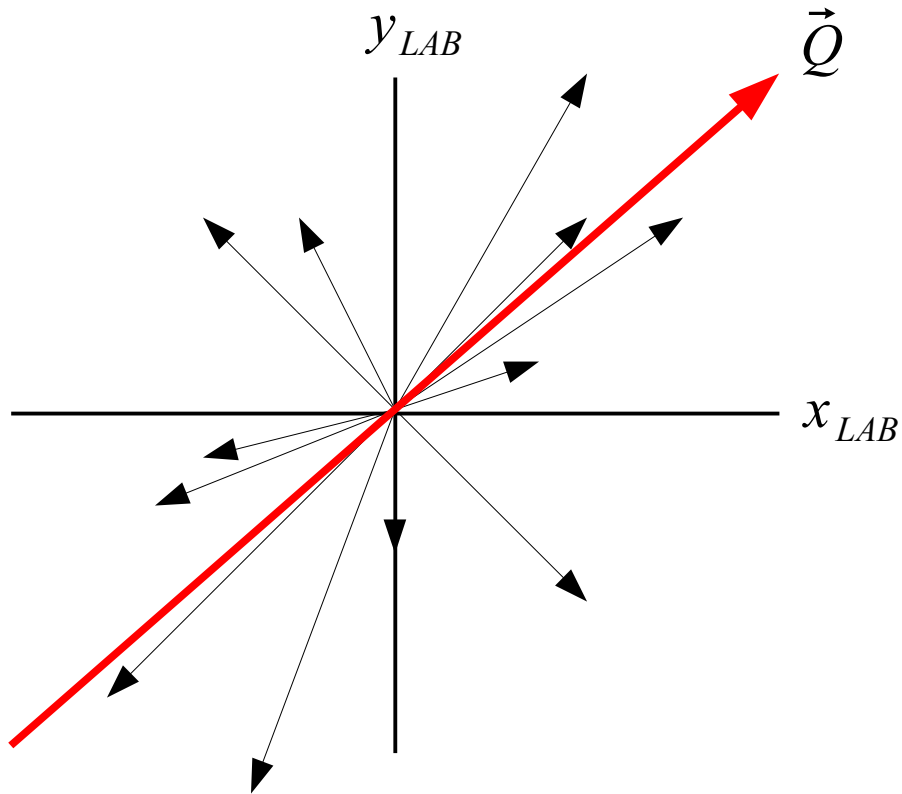
- Reconstructing the Reaction Plane
- HBT analysis and corrections for
 - effects from v_2 and number of particles on reaction plane resolution
 - effects from finite bin width
- Year 4 and Year 2 comparison, 200 GeV
- Year 4, 62.4 GeV results
- Excitation function

Motivation

- Energy dependence eccentricity at freeze-out constrains models
- Non-monotonic behavior may indicate interesting physics



Computing the reaction plane



Reaction plane vector components are

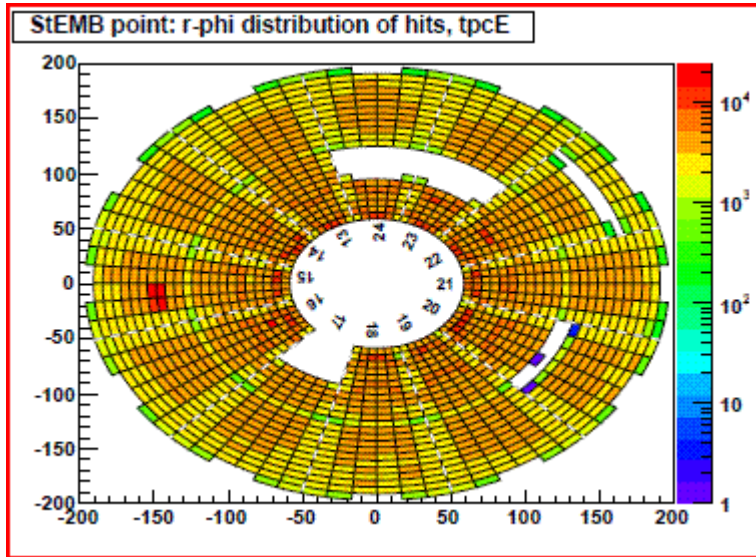
$$Q_x = \sum_{n=1}^{N_{particles}} w_{\phi} p_t \cos(2\phi_n)$$

$$Q_y = \sum_{n=1}^{N_{particles}} w_{\phi} p_t \sin(2\phi_n)$$

Finite number of particles and detector inefficiencies affect accuracy of reaction plane determination.

Use charged particles in TPC
(cuts on upcoming slide)

Correcting the reaction plane for detector effects



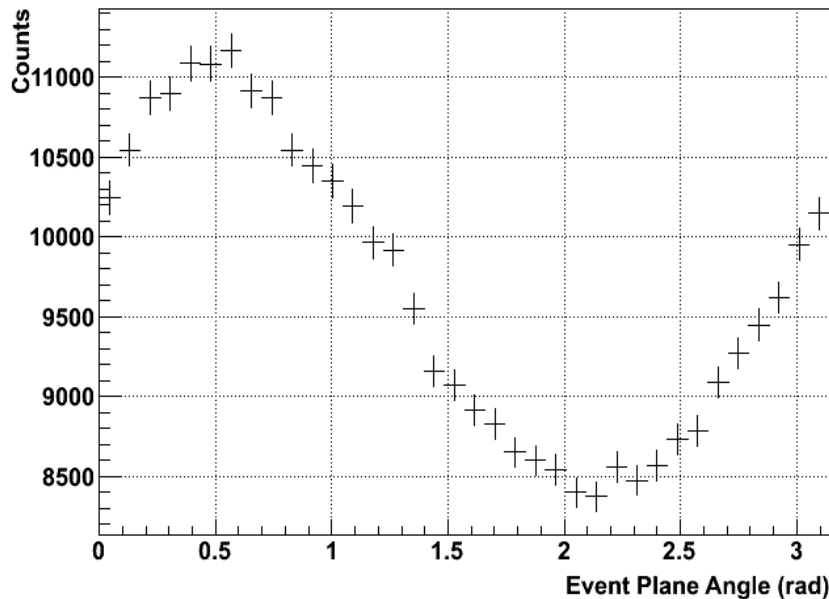
Track reconstruction inefficiency biases reaction plane in certain directions.

Phi-weight tracks with $w_\phi = \frac{\langle N \rangle_{\phi, avg}}{N_\phi}$

Phi weighting makes reaction plane distribution isotropic.

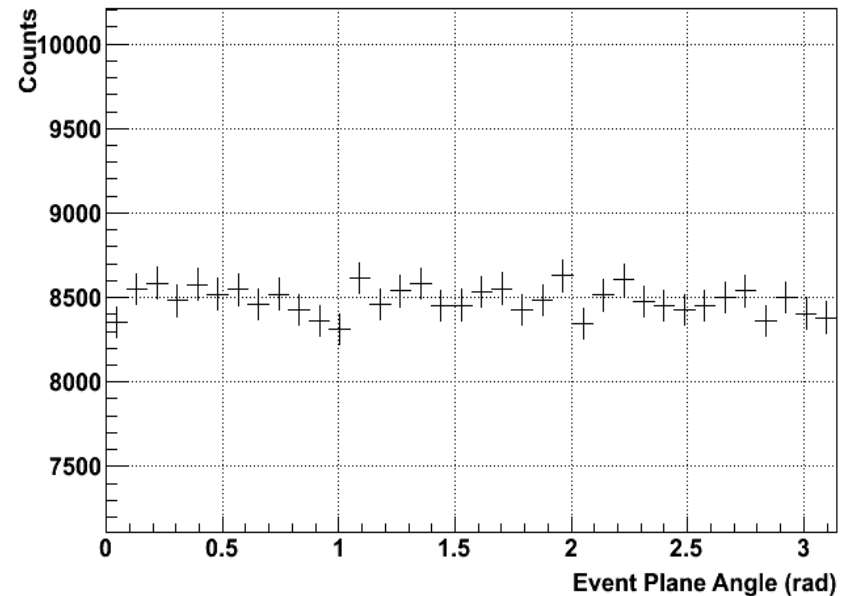
Reaction planes before

Reaction plane distribution (before phi-weights)



Reaction planes after

Reaction plane distribution (after phi-weights)



25%
effect

Event, track, and pair cuts

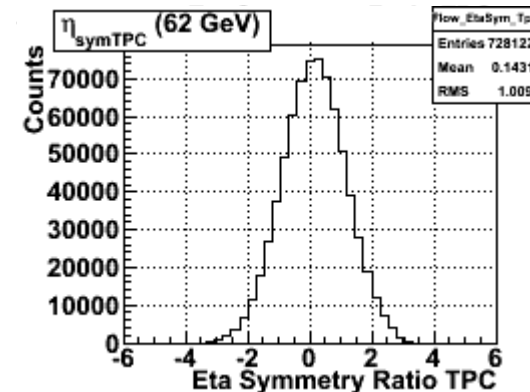
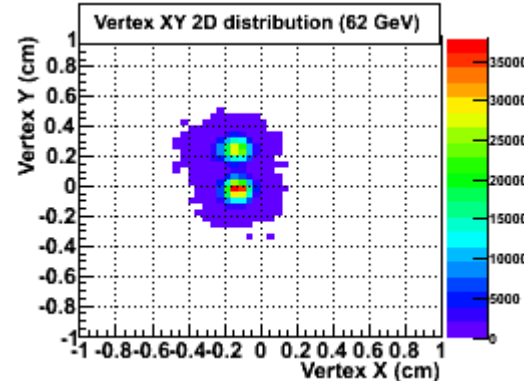
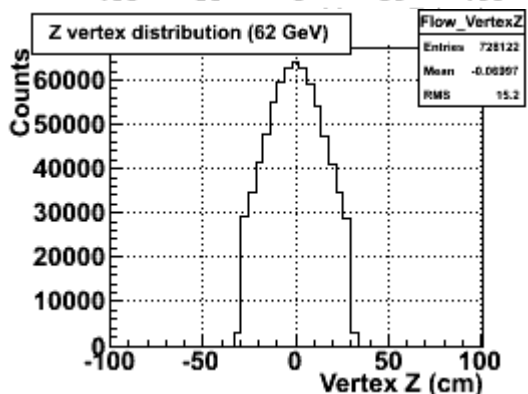
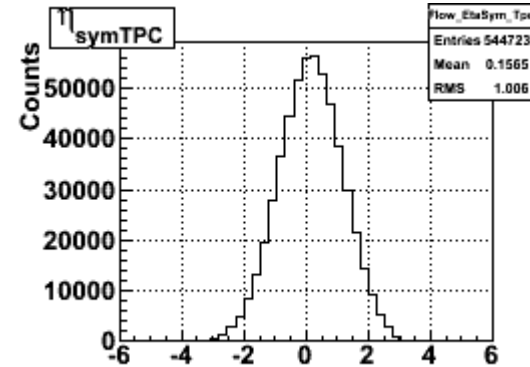
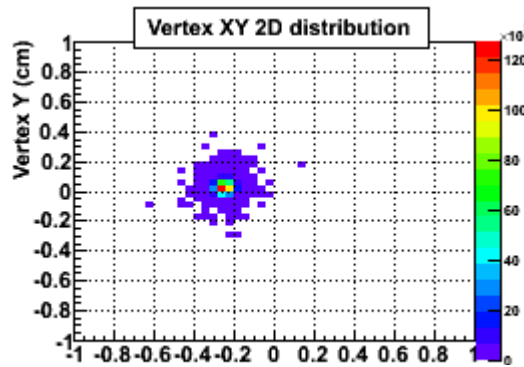
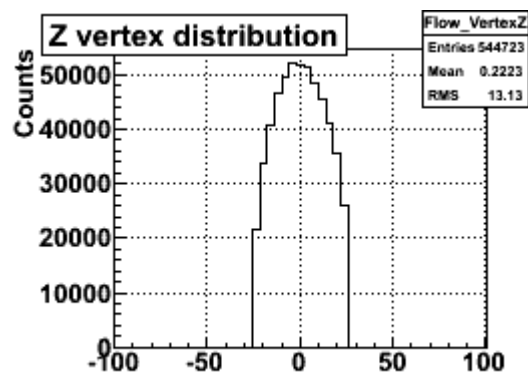
Event Cuts:

$|V_z| < 25$ cm (200 GeV)

$|V_z| < 30$ cm (62 GeV)

$|V_x|$ & $|V_y| < 1$ cm

$|\eta_{\text{SymTPC}}| < 3$



Track Cuts:

Reaction Plane

$0.15 < P_t < 12.0$ GeV/c

$|\eta| < 1.3$

$15 < n_{\text{FitPts}} < 50$

$0.52 < n_{\text{FitOverMax}} < 1.05$

HBT analysis

$0.1 < P_t < 1.0$ GeV/c

$|y| < 0.5$

$n_{\text{Hits}} \geq 10$

2D DCA < 3.0 cm

Sigma $\pi \leq 2$

Sigma k,p,e > 2

Pair Cuts:

HBT analysis

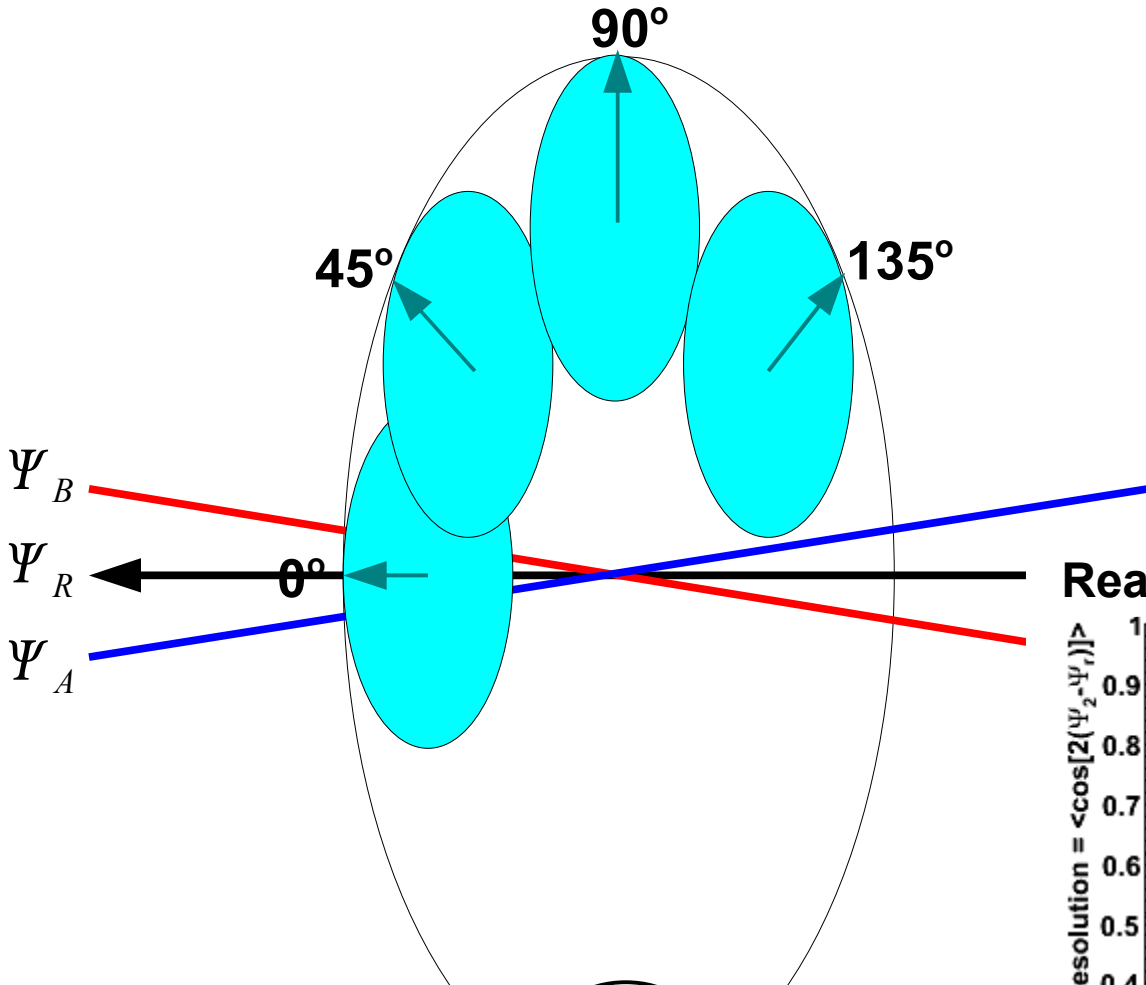
$0.15 < K_t < 0.6$ GeV/c

Anti-merging

maxFracMergedPair=0.1

$-0.5 < \text{Quality} < 0.6$

Reaction Plane resolution and finite angular bins



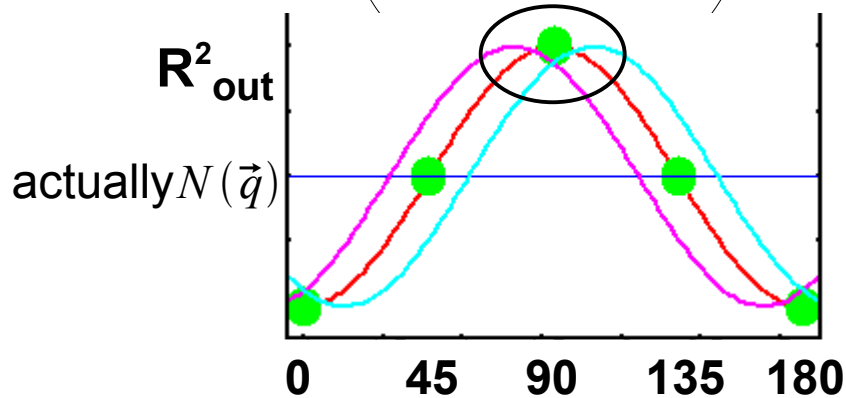
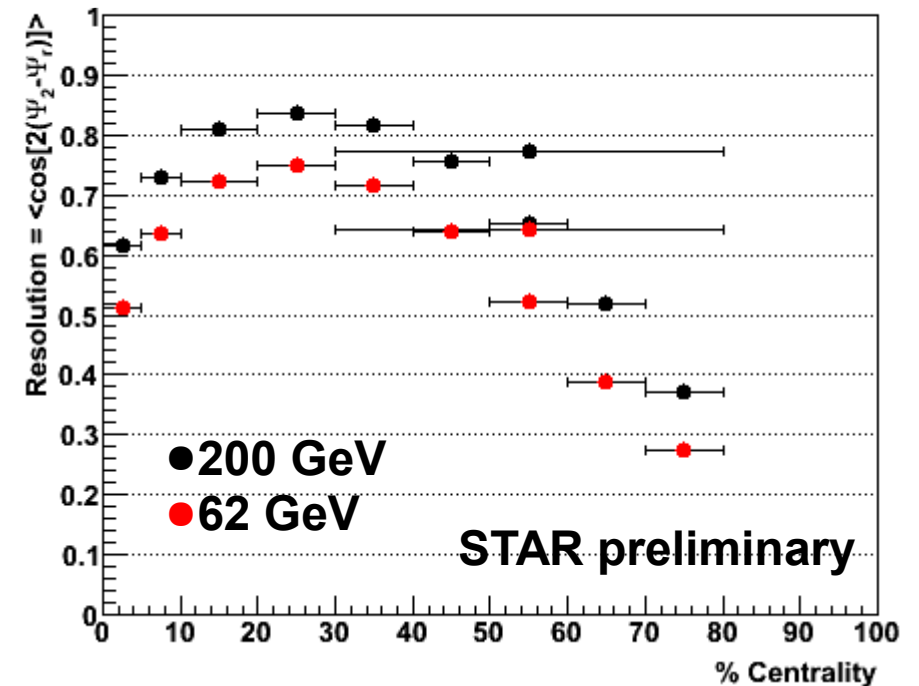
Oscillations reduced by
 • reaction plane resolution

$$\langle \cos[2(\Psi_m - \Psi_R)] \rangle$$

• and finite angular bins

$$\frac{\sin(n \Delta/2)}{n \Delta/2}$$

Reaction Plane resolution vs. Centrality



Correction scheme

Expand the correlation function with Fourier series

$$N_{\text{exp}}(\vec{q}, \Phi_j) = N_0^{\text{exp}}(\vec{q}) + 2 \sum_{n=1}^{n_{\text{bins}}/2} [N_{c,n}^{\text{exp}}(\vec{q}) \cos(n \Phi_j) + N_{s,n}^{\text{exp}}(\vec{q}) \sin(n \Phi_j)]$$

where

$$N_{c,n}^{\text{exp}}(\vec{q}) = \frac{1}{n_{\text{bins}}} \sum_{j=1}^{n_{\text{bins}}} N_{\text{exp}}(\vec{q}, \Phi_j) \cos(n \Phi_j)$$

$$N_{s,n}^{\text{exp}}(\vec{q}) = \frac{1}{n_{\text{bins}}} \sum_{j=1}^{n_{\text{bins}}} N_{\text{exp}}(\vec{q}, \Phi_j) \sin(n \Phi_j)$$

The true numerator is then given by

$$N(\vec{q}, \Phi_j) = N_{\text{exp}}(\vec{q}) + 2 \sum_{n=1}^{n_{\text{bins}}/2} \zeta_{n,m} [N_{c,n}^{\text{exp}}(\vec{q}) \cos(n \Phi_j) + N_{s,n}^{\text{exp}}(\vec{q}) \sin(n \Phi_j)]$$

where the correction term is

$$\zeta_{n,m} = \frac{n \Delta/2}{\sin(n \Delta/2)} \frac{1}{\langle \cos[n(\Psi_m - \Psi_R)] \rangle} - 1$$

Repeat for denominator and Coulomb “interaction” histogram.

Correction Method from

U. Heinz, A. Hummel, M.A. Lisa, and U. A. Wiedemann, Phys. Rev. C 52, 2694 (1995).₈

Fitting procedure

$$C(q_o, q_s, q_l) = \frac{N(\vec{q})}{D(\vec{q})} = (1 - \lambda) + \lambda K_{Coul}(q_{inv}) (1 + e^{-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2 - 2q_o q_s R_{os}^2})$$

Refit with
 $\lambda = \langle \lambda \rangle_{avg}$

Centrality = 30-80% Kt = 0

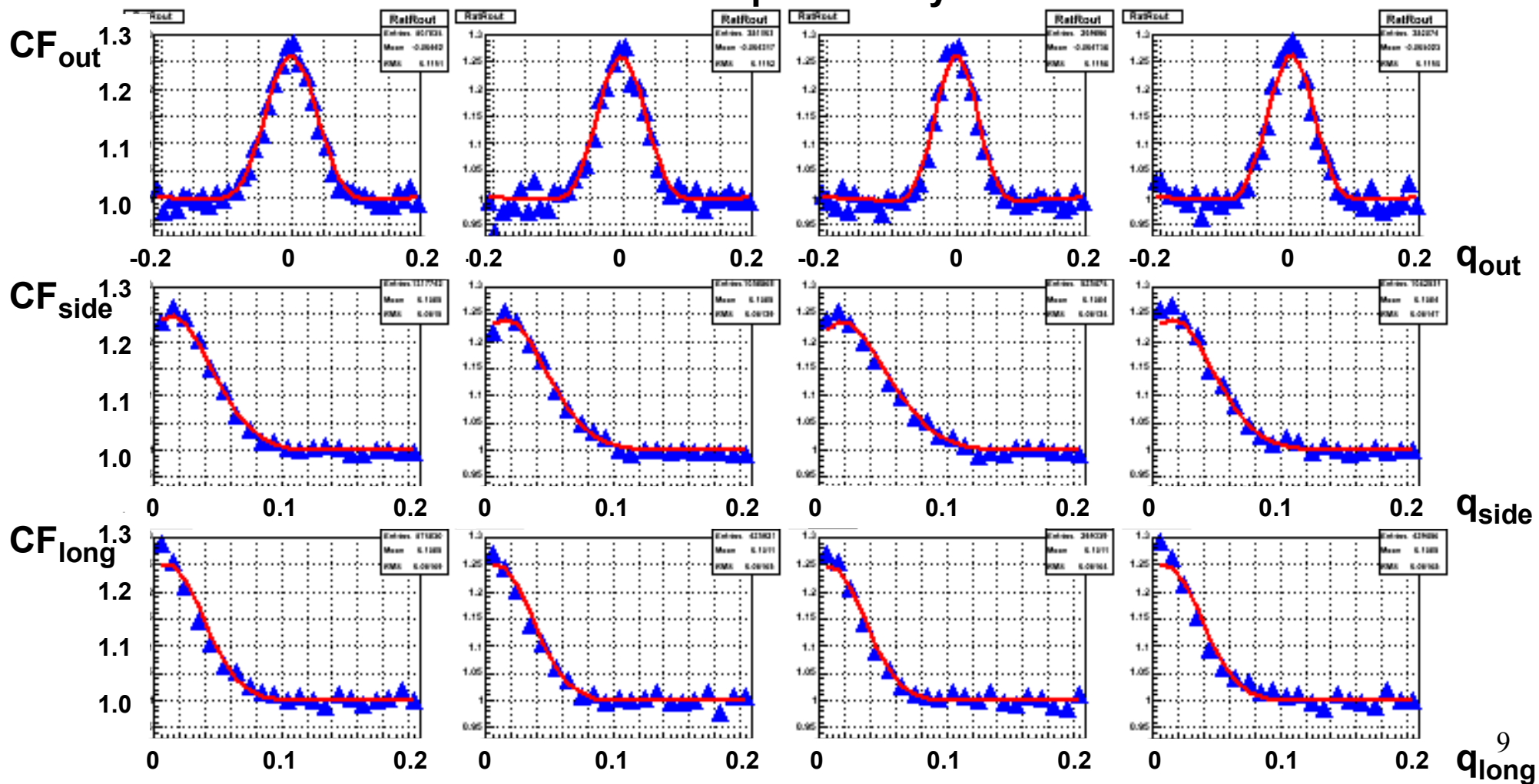
Au+Au 200 GeV

Phi = 0

Phi = 90

Phi = 135

STAR preliminary



Computing Fourier Coefficients

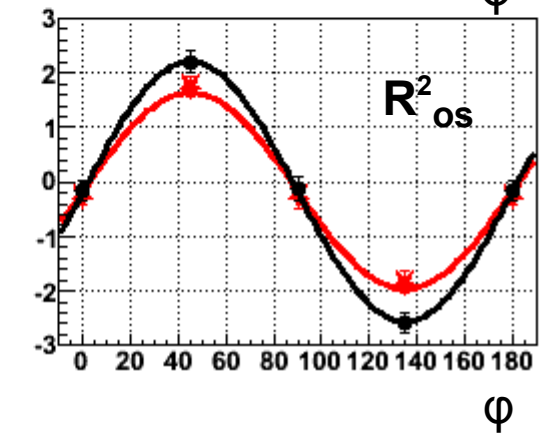
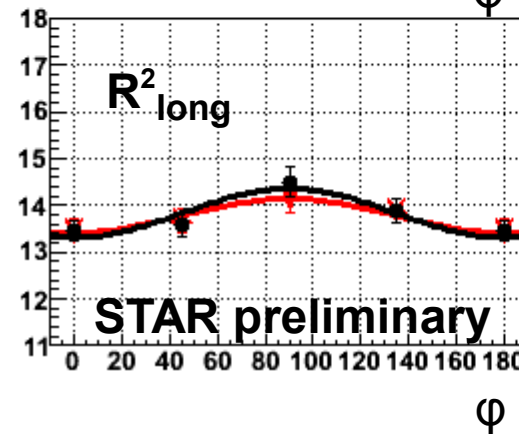
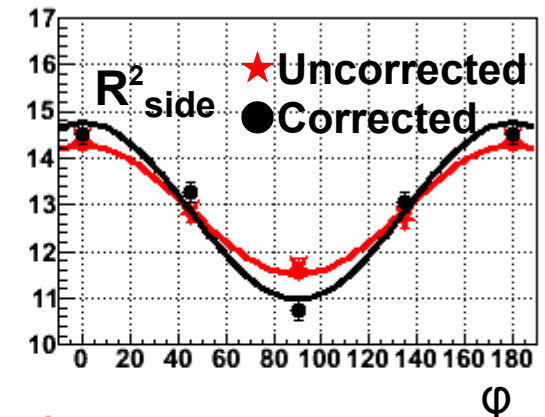
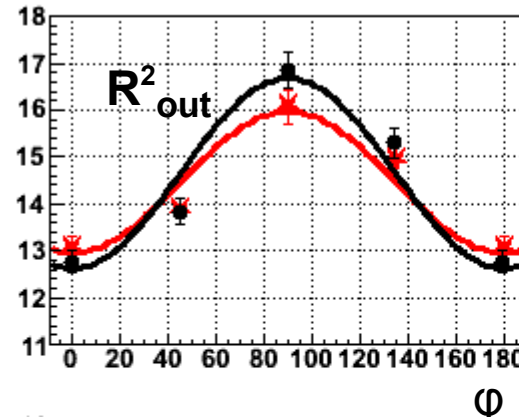
Fourier coefficients
computed from radii:

$$R_{0,i}^2 = \sum_{j=1}^{N_{bins}} R_i^2(\Phi_j) \quad i=o, s, l, os$$

$$R_{2,i}^2 = \sum_{j=1}^{N_{bins}} R_i^2(\Phi_j) \cos(2\Phi_j) \quad i=o, s, l$$

$$R_{2,i}^2 = \sum_{j=1}^{N_{bins}} R_i^2(\Phi_j) \sin(2\Phi_j) \quad i=os$$

Au+Au 200 GeV
Oscillations for 20-30% Centrality
and $K_t = 0.35-0.60$ GeV/c



Computing eccentricity at freeze-out

Eccentricity from Blast-wave model:

$$\varepsilon = \frac{R_y^2 - R_x^2}{R_y^2 + R_x^2} = 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$

Eccentricity equation derived in
Retiere and Lisa, nucl-th/0312024

K_t Average Method:

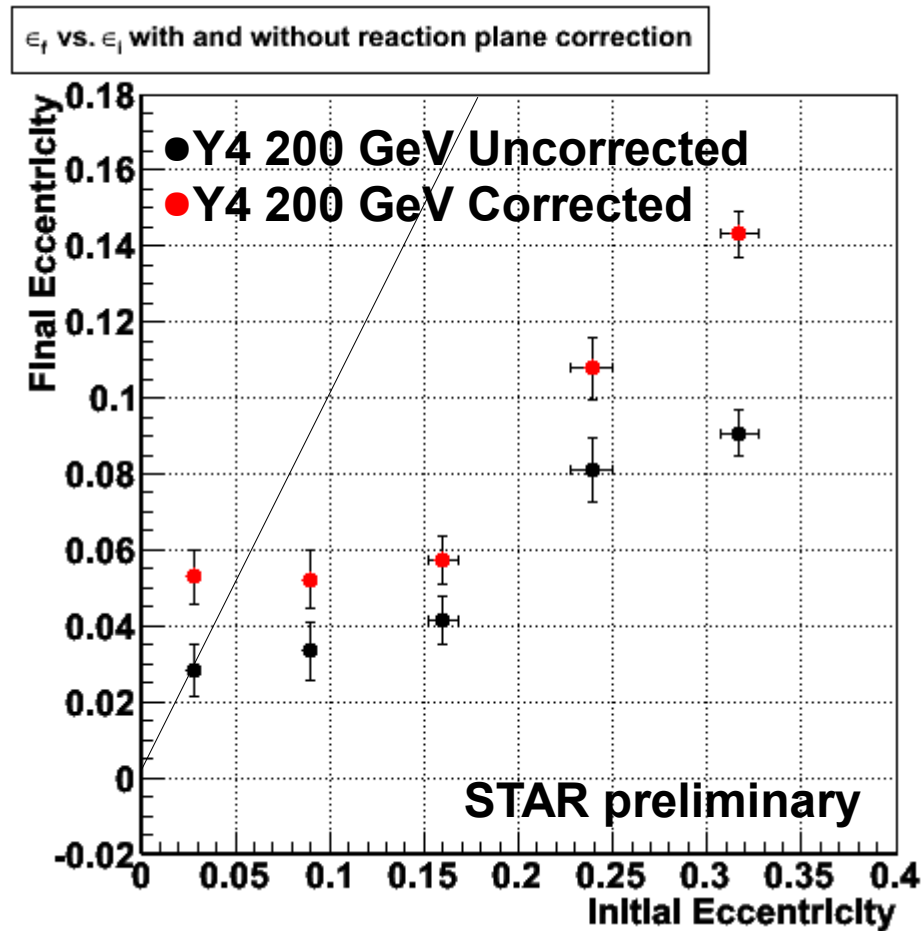
- Compute ε_f for the three K_t bins separately
- Simply average

$$\varepsilon_{KtAvg} = \frac{(\varepsilon_{Kt1} + \varepsilon_{Kt2} + \varepsilon_{Kt3})}{3}$$

K_t Integrated Method:

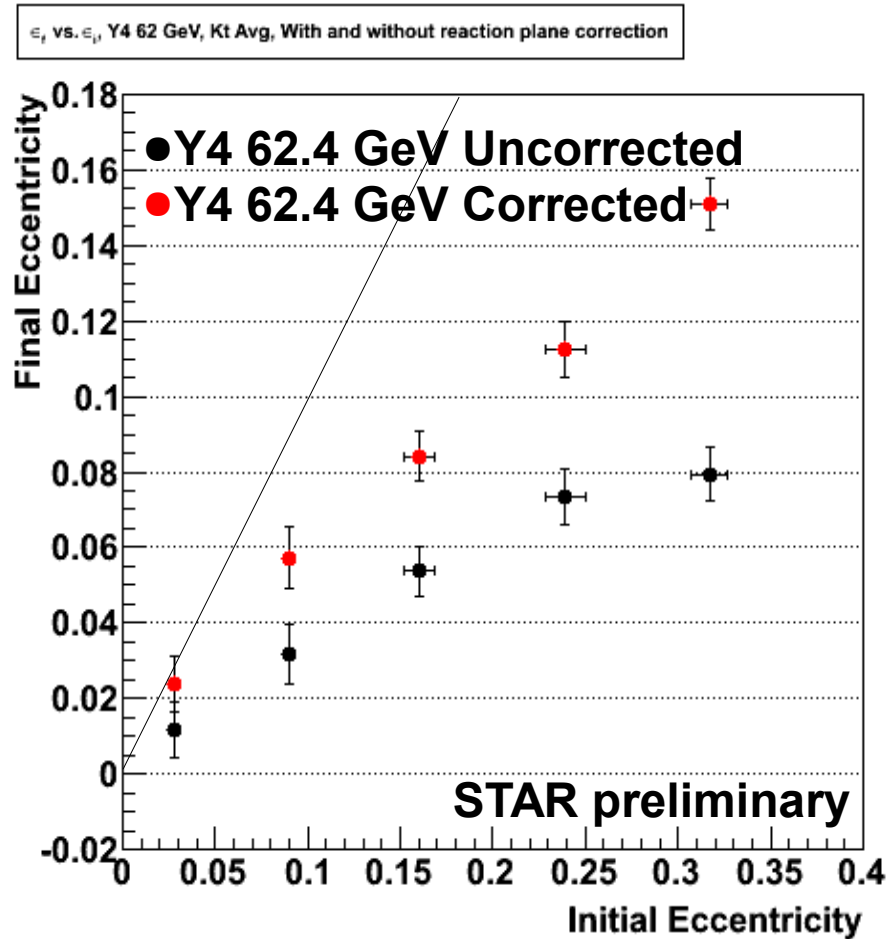
- Compute ε_f for one K_t Integrated correlation function

Y4 at 200 GeV Uncorrected vs Corrected



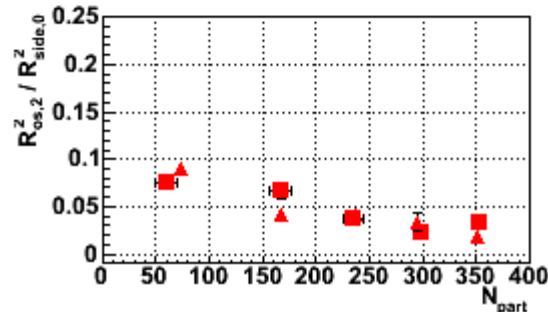
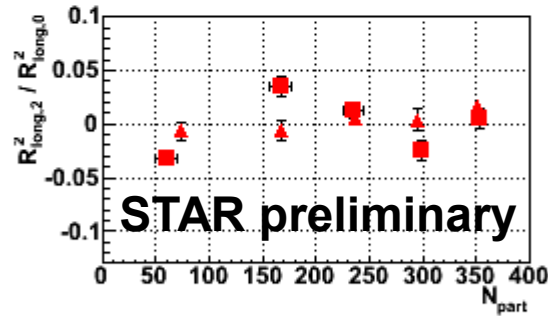
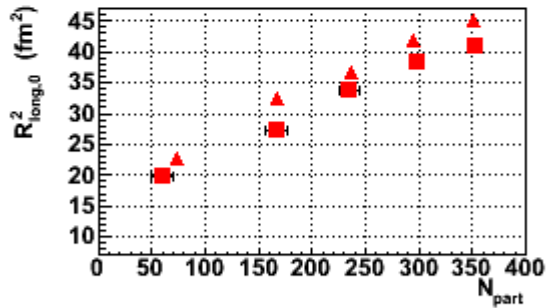
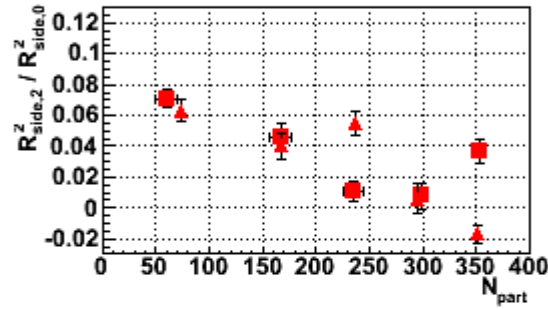
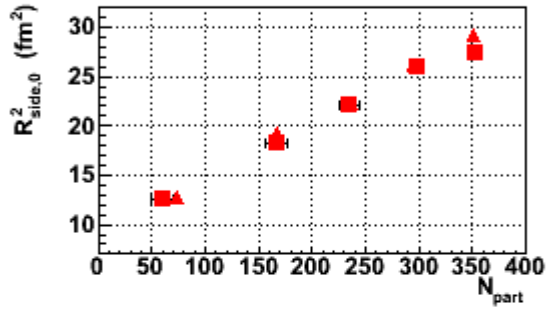
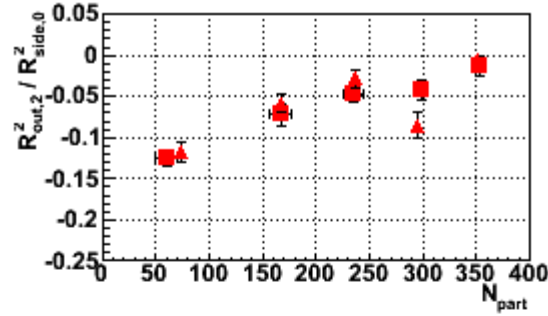
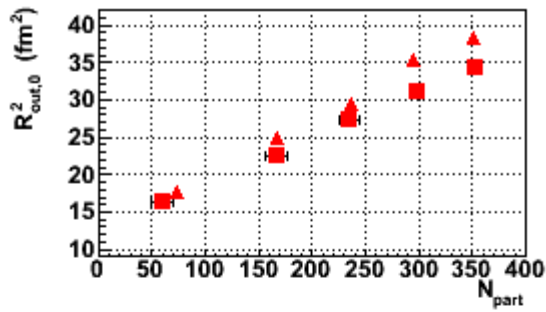
The correction scheme increases the oscillations and therefore the eccentricities.

Y4 at 62.4 GeV Uncorrected vs Corrected



The correction scheme increases the oscillations and therefore the eccentricities.

Y4 vs Y2 at 200 GeV



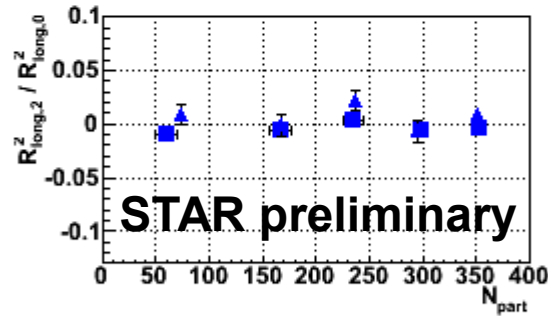
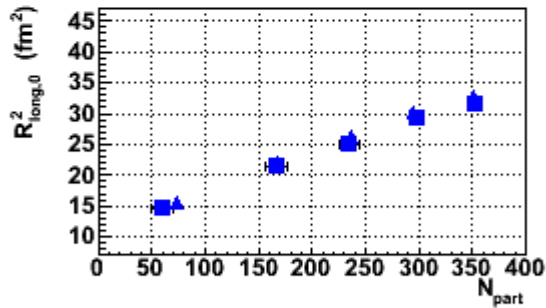
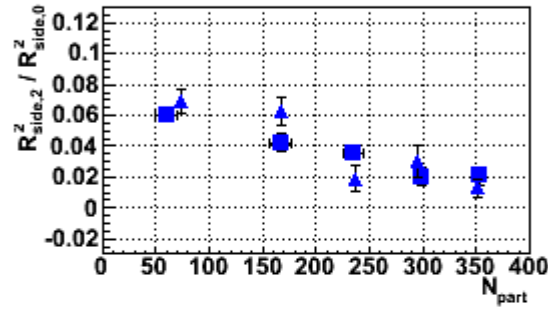
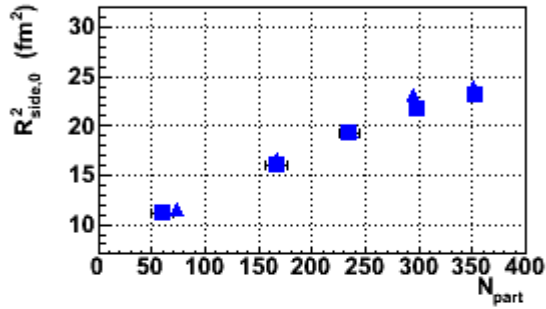
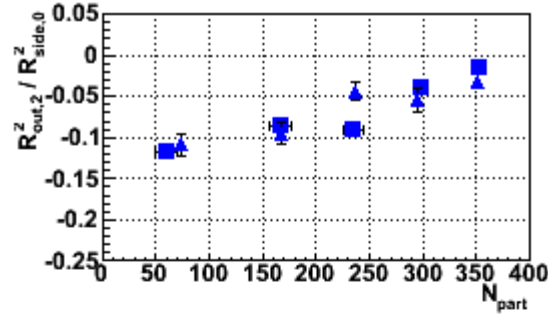
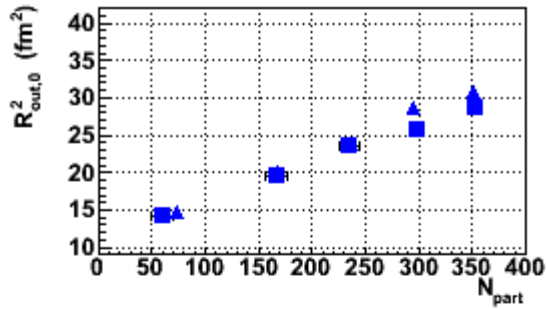
▲ Y2, 200 GeV
 ■ Y4, 200 GeV
 Fourier Coefficients vs. Npart
 Y4 and Y2 200 GeV
 Kt = 0.15 - 0.25
 Lambda fixed
 RP corrected

- Lowest K_t bin
- 0th order R_{out} and R_{long} a bit low
- Some differences present in the 2nd order / 0th order

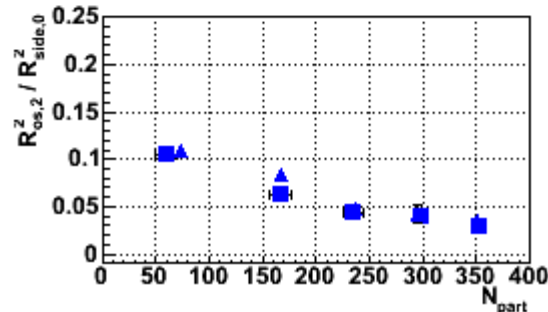
STAR preliminary

Year 2 data from
 J. Adams *et al.* (STAR Collaboration),
 Phys. Rev. Lett. **93**, 012301 (2004)

Y4 vs Y2 at 200 GeV



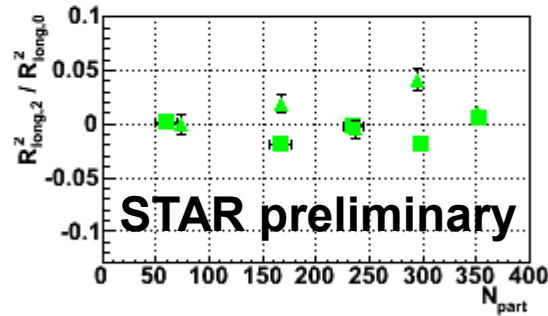
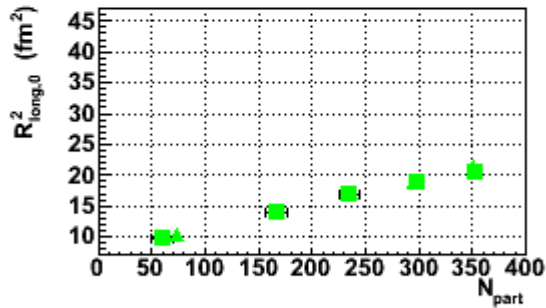
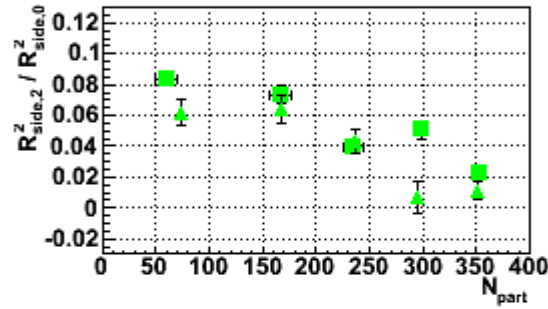
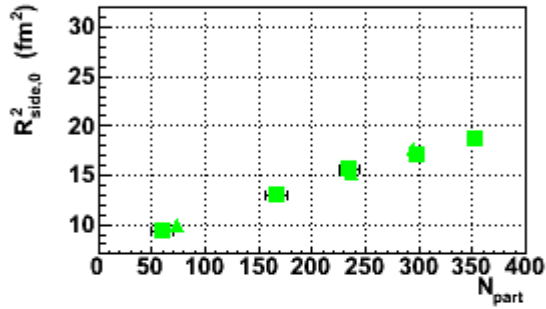
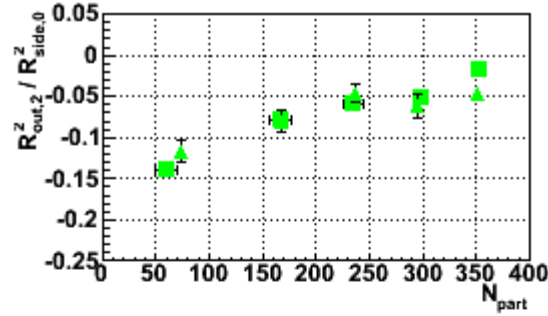
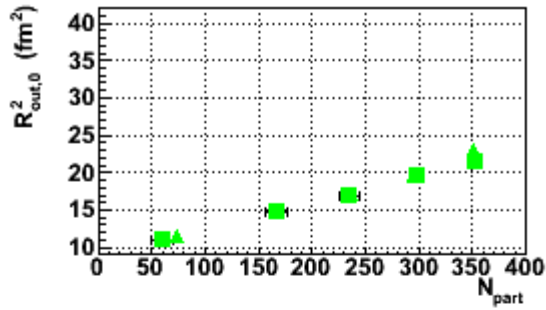
▲ Y2, 200 GeV
 ■ Y4, 200 GeV
 Fourier Coefficients vs. Npart
 Y4 and Y2 200 GeV
 $K_t = 0.25 - 0.35$
 Lambda fixed
 RP corrected



- Middle K_t bin
- 0th order agree pretty well
- Some differences present in the 2nd order / 0th order

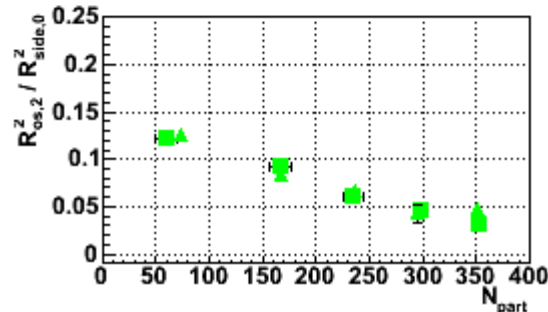
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Y4 vs Y2 at 200 GeV



▲ Y2, 200 GeV
■ Y4, 200 GeV

Fourier Coefficients vs. Npart
Y4 and Y2 200 GeV
Kt = 0.35 - 0.6
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RP corrected

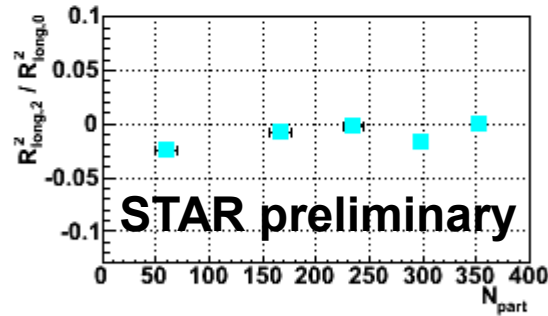
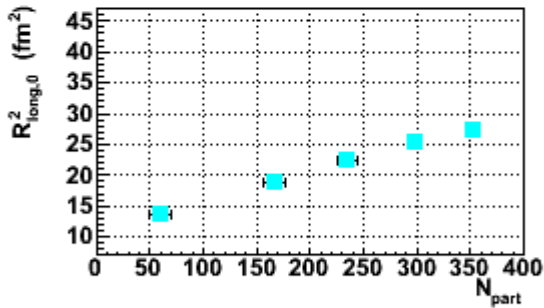
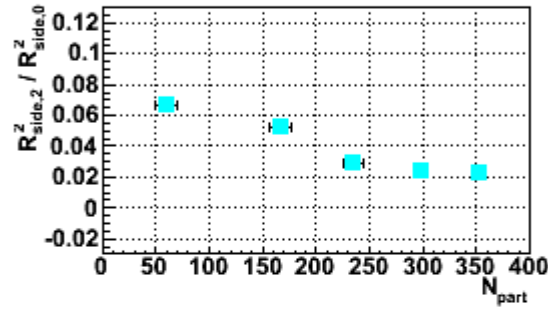
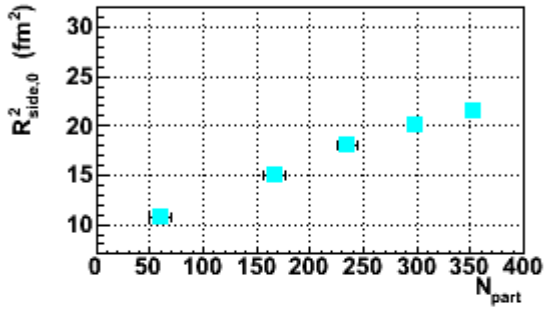
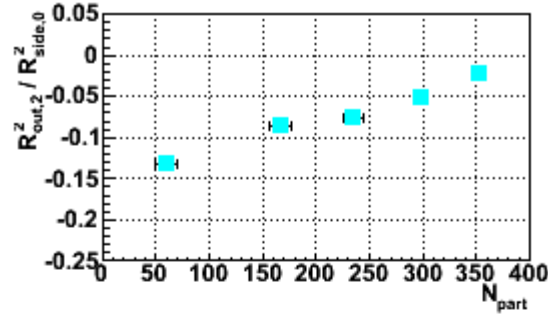
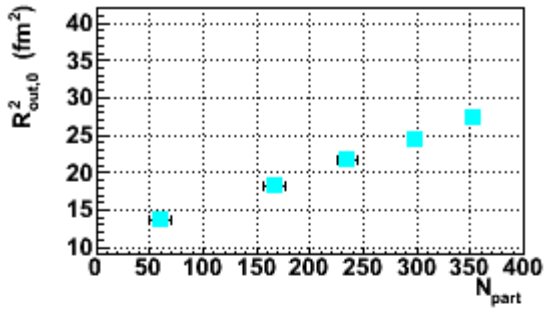


- Highest K_t bin
- 0th agree well
- Some differences present in the 2nd order / 0th order

Year 2 data from
J. Adams *et al.* (STAR Collaboration),
Phys. Rev. Lett. **93**, 012301 (2004)

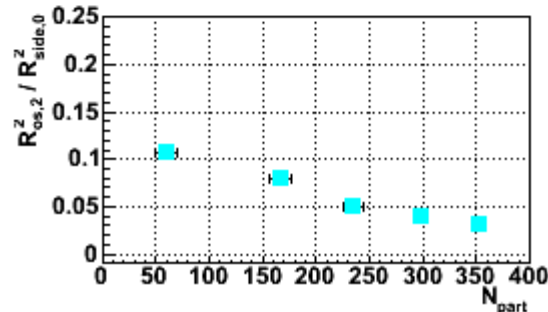
Y4 at 200 GeV

• K_t Integrated



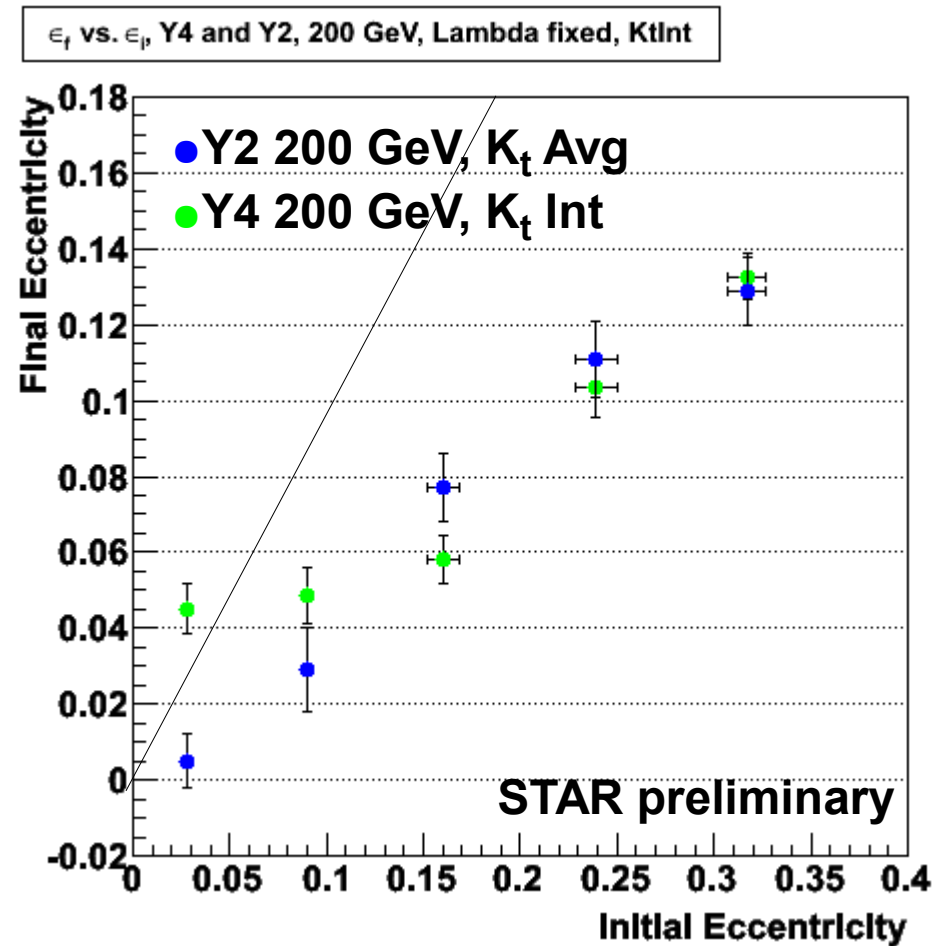
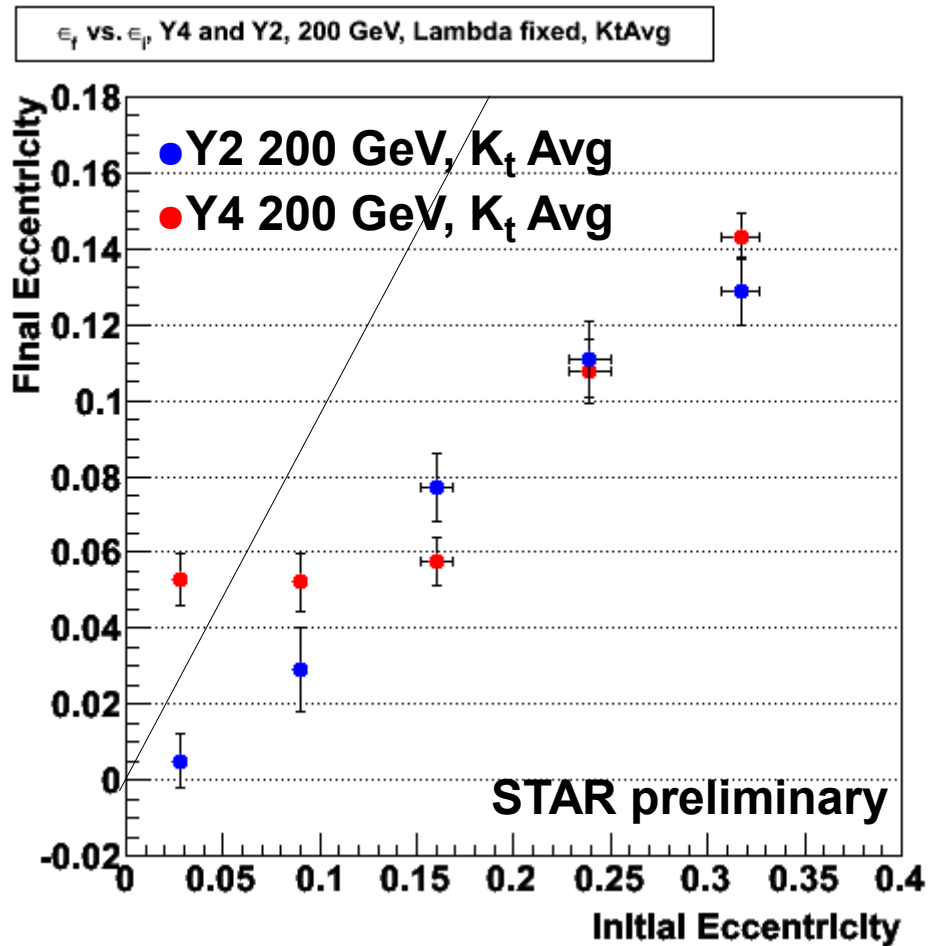
■ Y4, 200 GeV

Fourier Coefficients vs. Npart
 Y4 and Y2 200 GeV
 $K_t = 0.15 - 0.6$
 Lambda fixed
 RP corrected



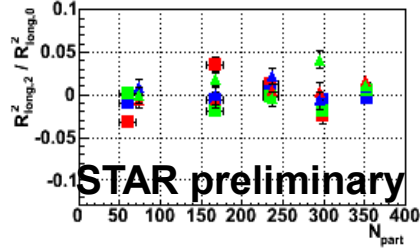
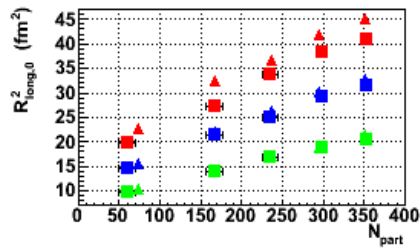
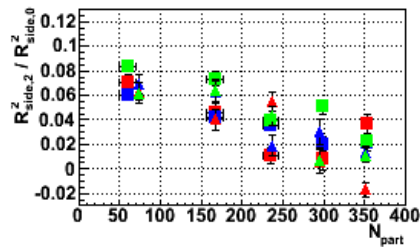
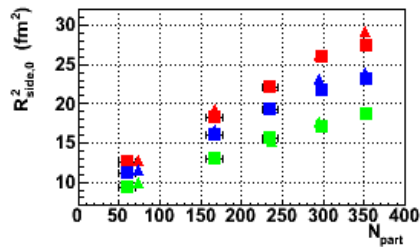
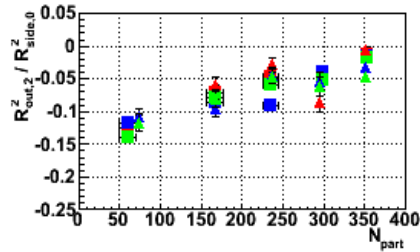
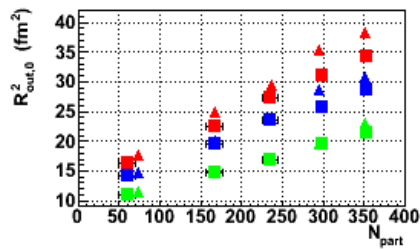
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Y4 vs Y2 at 200 GeV

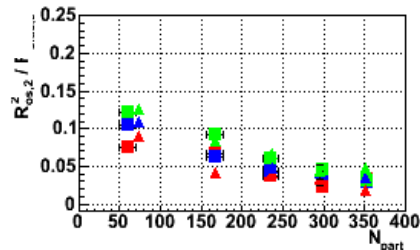


- Some differences (most central bin in particular)
- Physics extracted comes from 3rd and 4th bins which yield similar final eccentricity.

Fit Range Effects

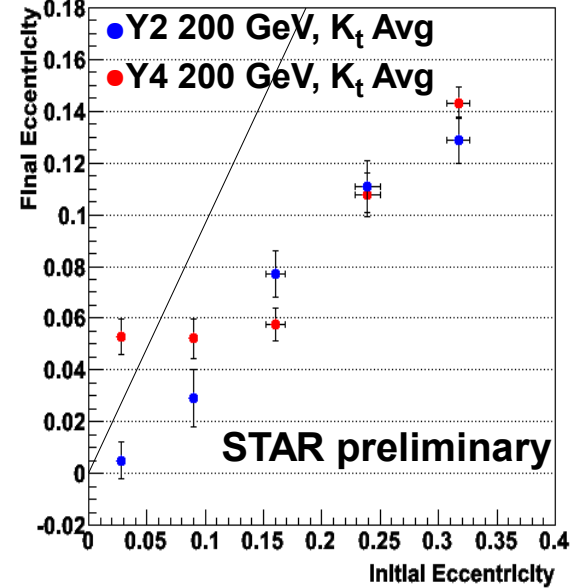


▲ ▲ ▲ Y2, 200 GeV
■ ■ ■ Y4, 200 GeV
 Fourier Coefficients vs. Npart
 Y4 and Y2 200 GeV
 Kt Comparison
 Lambda fixed
 RP corrected



- Fit Range: $q < 0.15$ GeV/c
- Lowest K_t , 0th order disagree

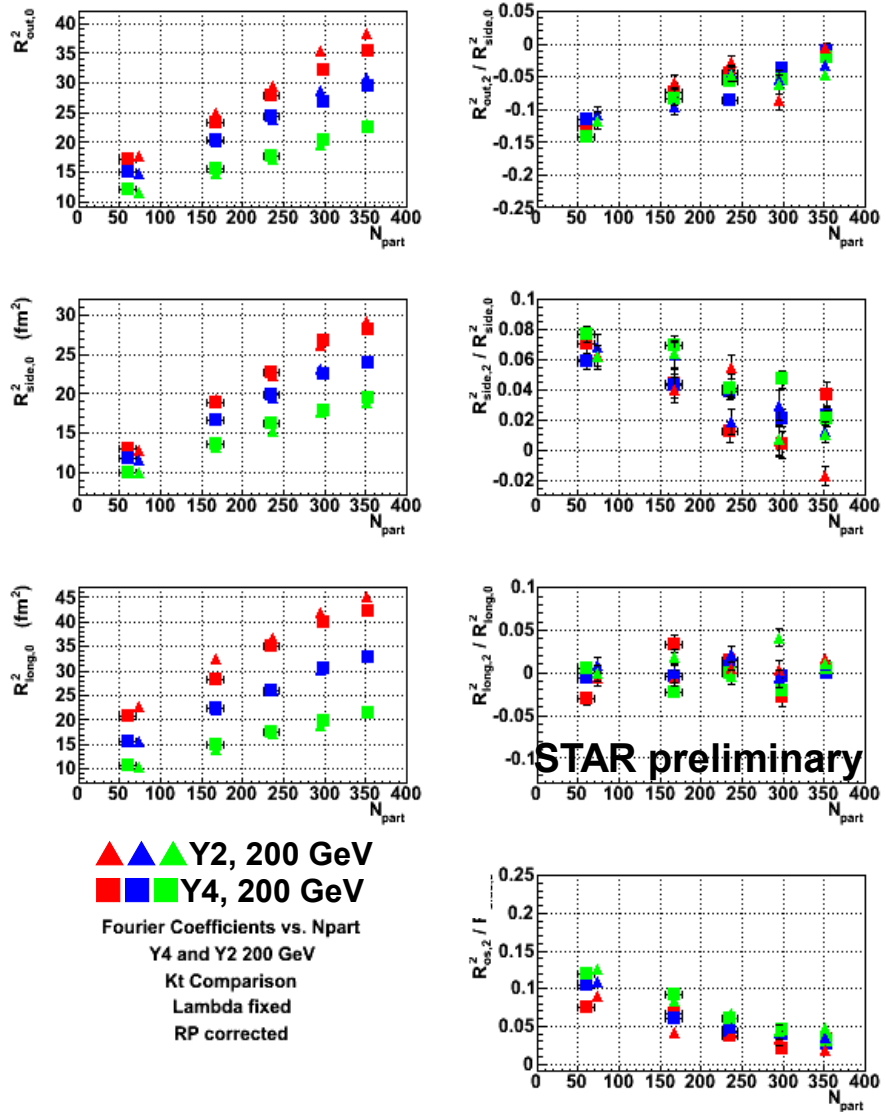
ϵ_f vs. ϵ_p , Y4 and Y2, 200 GeV, Lambda fixed, Kt Avg



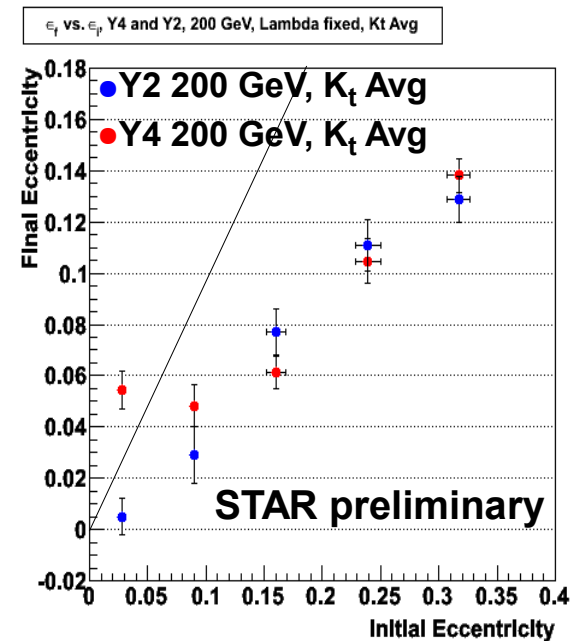
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Fit Range Effects



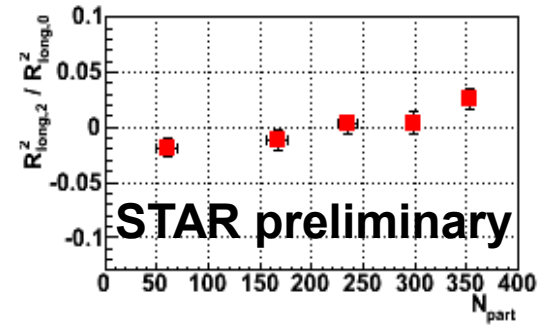
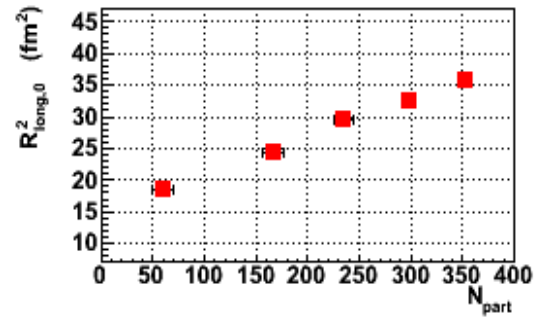
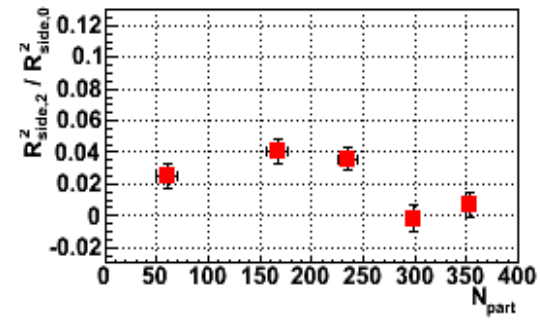
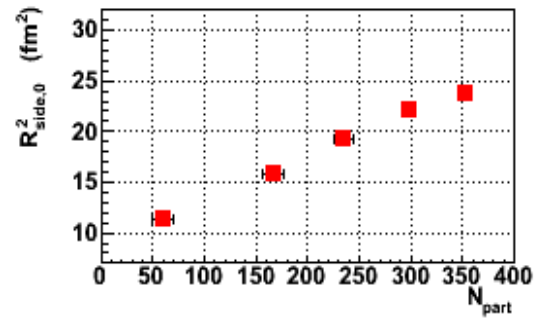
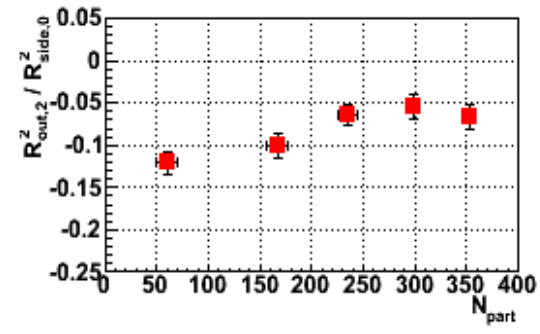
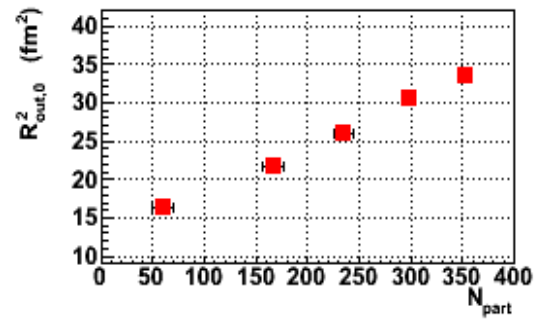
- Fit Range: $q < 0.12$ GeV/c
- Lowest K_t , 0th order agree better
- ϵ almost unchanged



Year 2 data from
 J. Adams *et al.* (STAR Collaboration), Phys. Rev. Lett. **93**, 012301 (2004)

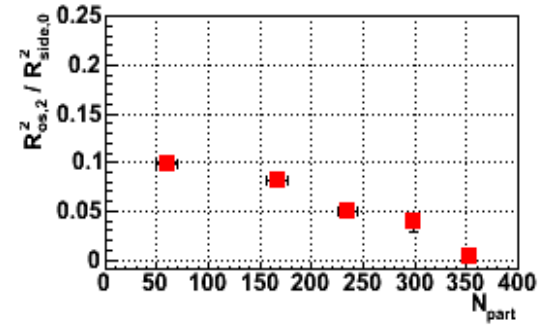
Y4 at 62.4 GeV

- Fit Range: $q < 0.15$ GeV/c
- Lowest K_t bin
- Some scatter in $R_{s,2}^2 / R_{s,0}^2$



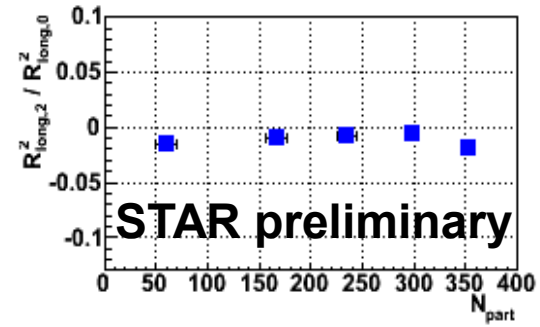
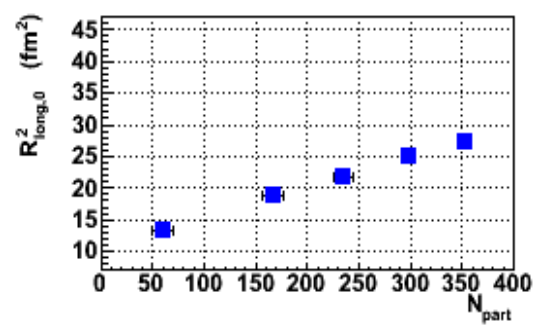
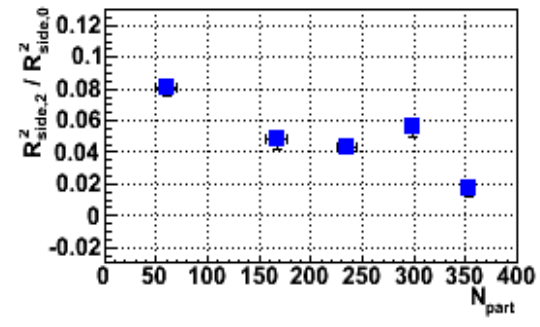
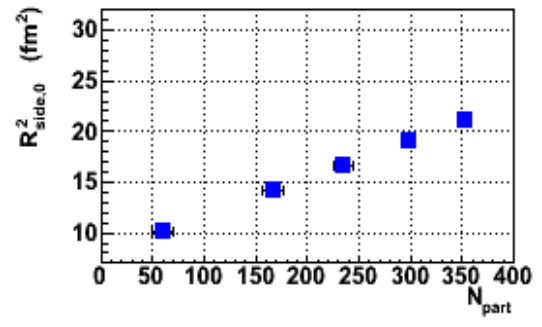
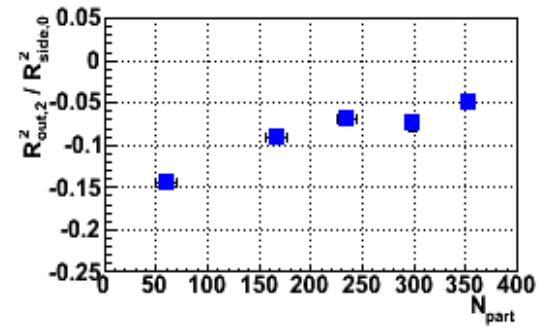
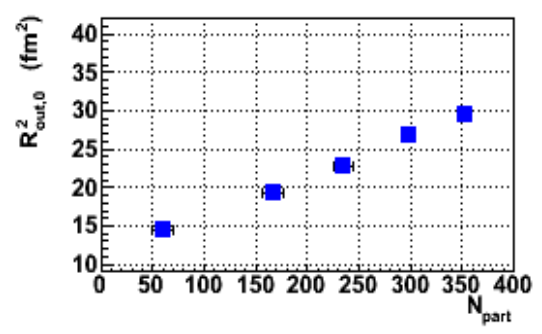
■ Y4, 62.4 GeV

Fourier Coefficients vs. Npart
 Y4 62 GeV
 $K_t = 0.15 - 0.25$
 Lambda fixed
 RP corrected



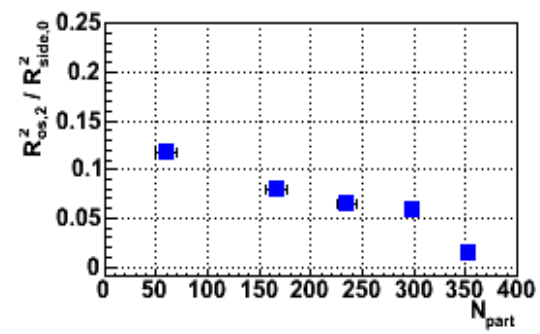
Y4 at 62.4 GeV

- Fit Range: $q < 0.15$ GeV/c
- Middle K_t bin
- Some scatter in $R_{s,2}^2 / R_{s,0}^2$



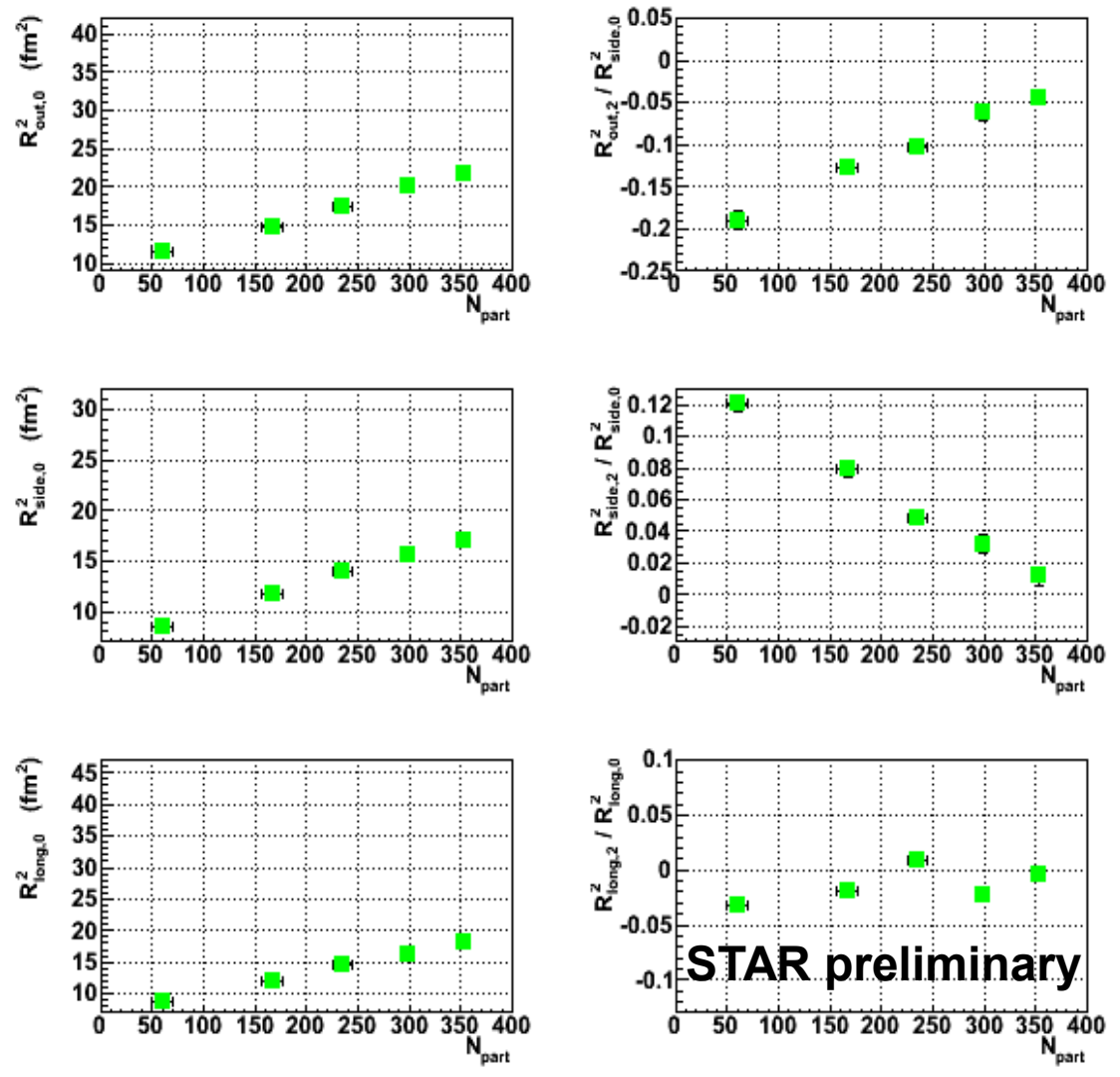
■ Y4, 62.4 GeV

Fourier Coefficients vs. Npart
 Y4 62 GeV
 $K_t = 0.25 - 0.35$
 Lambda fixed
 RP corrected



Y4 at 62.4 GeV

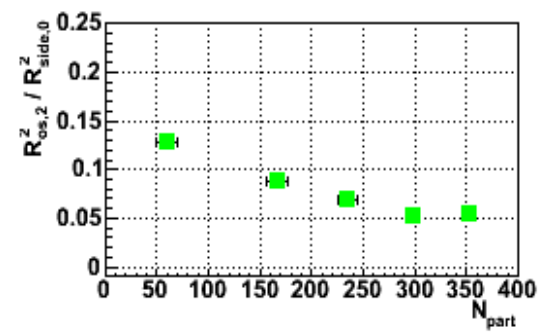
- Fit Range: $q < 0.15$ GeV/c
- Highest K_t bin



STAR preliminary

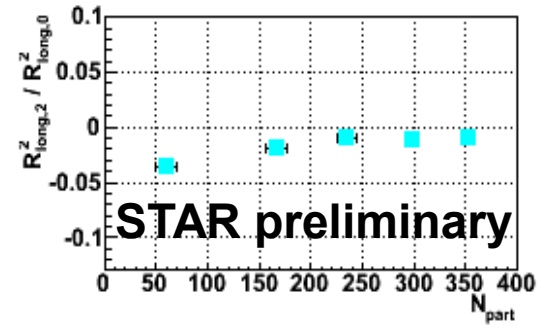
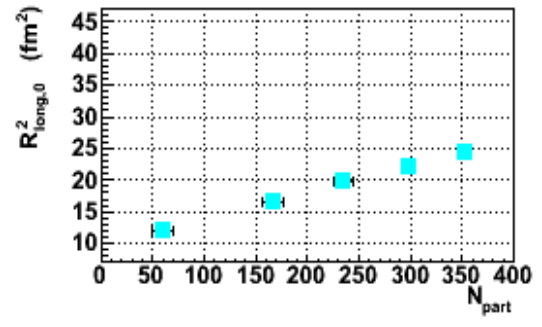
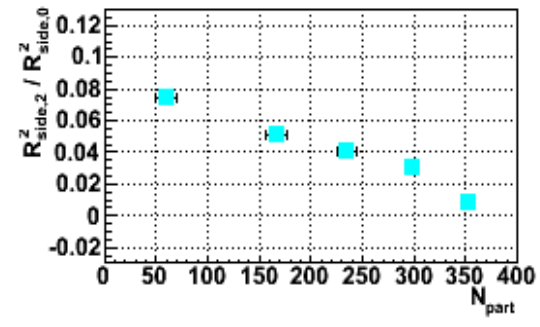
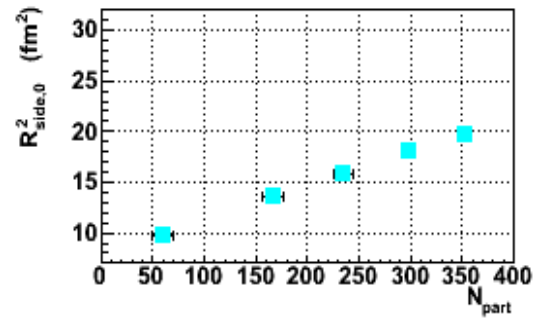
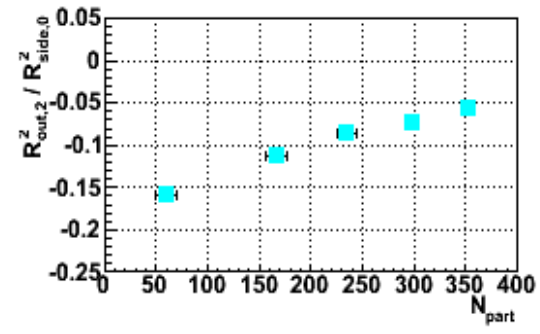
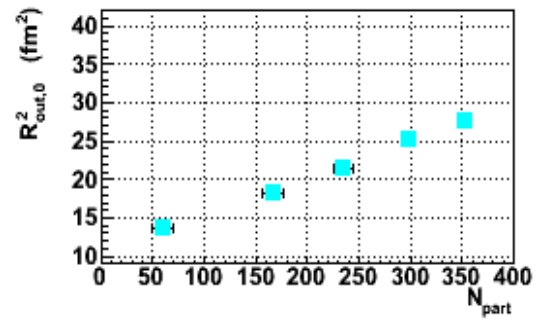
■ Y4, 62.4 GeV

Fourier Coefficients vs. Npart
 Y4 62 GeV
 $K_t = 0.35 - 0.6$
 Lambda fixed
 RP corrected



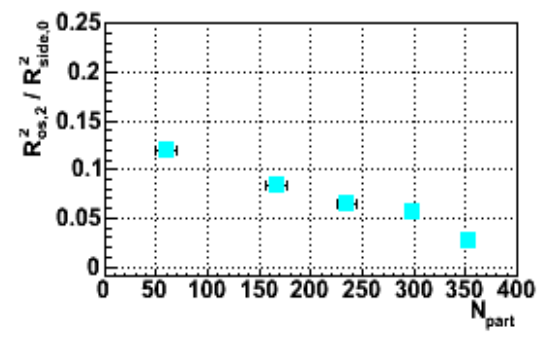
Y4 at 62.4 GeV

- Fit Range: $q < 0.15$ GeV/c
- K_t Integrated

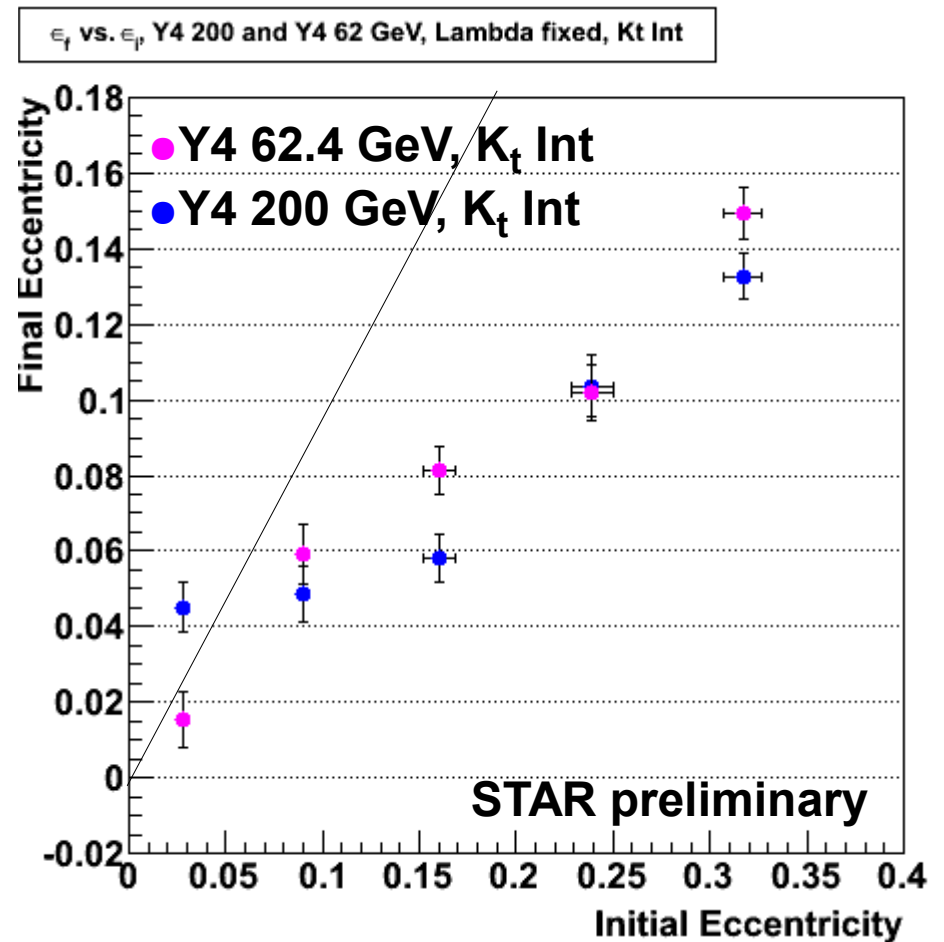
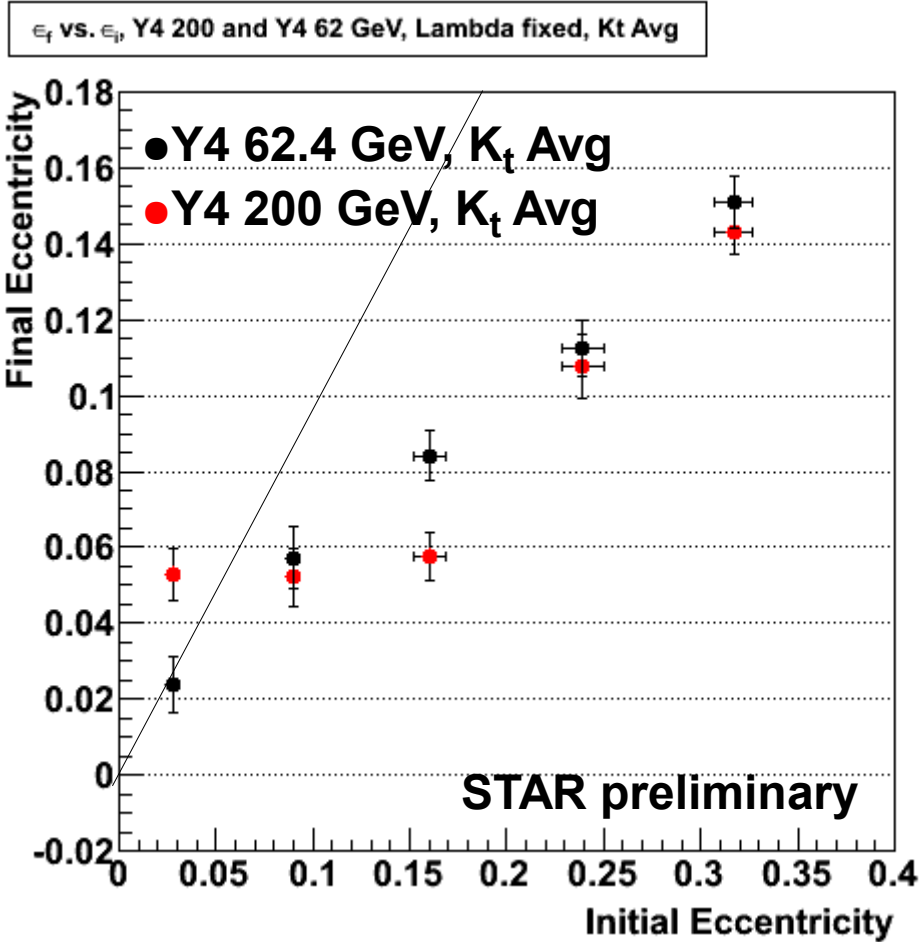


■ Y4, 62.4 GeV

Fourier Coefficients vs. Npart
 Y4 62 GeV
 $K_t = 0.15 - 0.6$
 Lambda fixed
 RP corrected

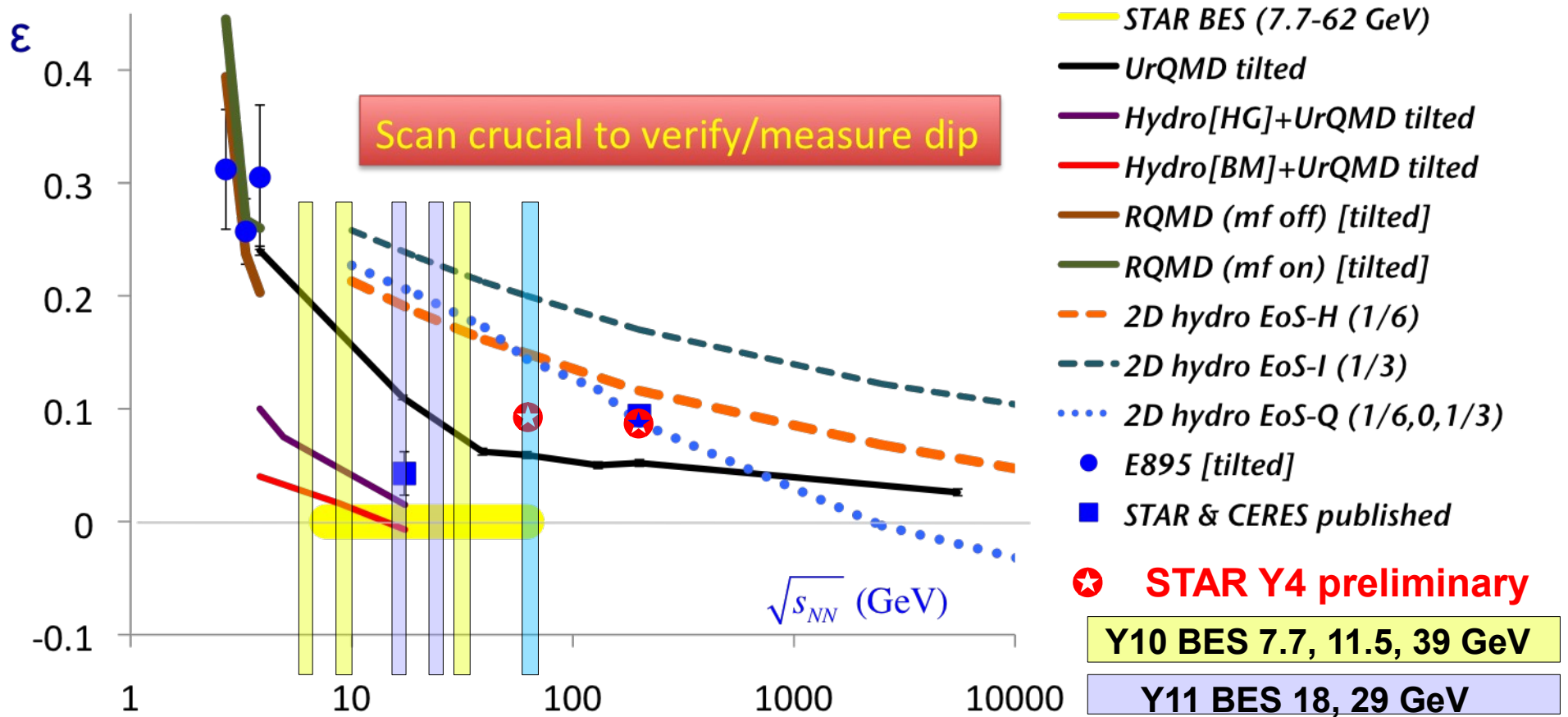


Y4 at 62.4 and 200 GeV



Excitation Function

- Y4 62.4 GeV greater than Y4 200 GeV (both K_t Avg and K_t Int cases)
- Y4 62.4 GeV slightly greater than Y2 200 GeV (K_t Avg case)

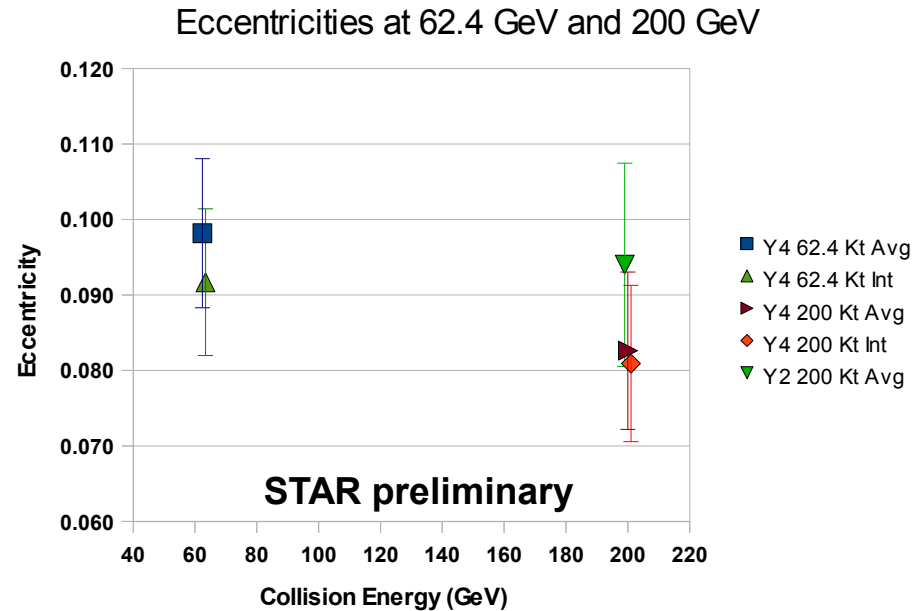


Conclusions

- Preliminary Y4 62.4 GeV and Y4 200 GeV results suggest the excitation function is constant or slightly decreases at the higher energy.
- Further systematic studies needed.
- Need lower energies to determine shape of excitation function.
- Beam Energy Scan energies will fill in the excitation function
 - 7.7 GeV, 11.5 GeV, 39 GeV – Analysis in progress
 - 18 GeV, 29 GeV – Scheduled for Run 11

Backup slides

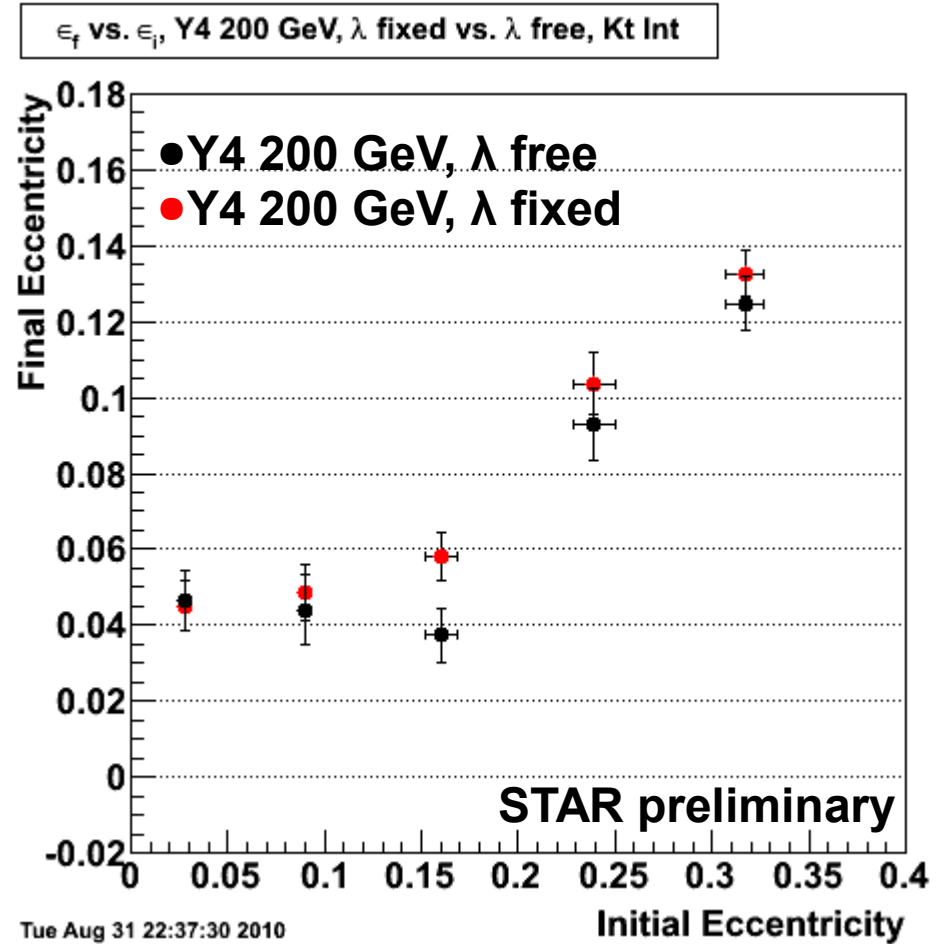
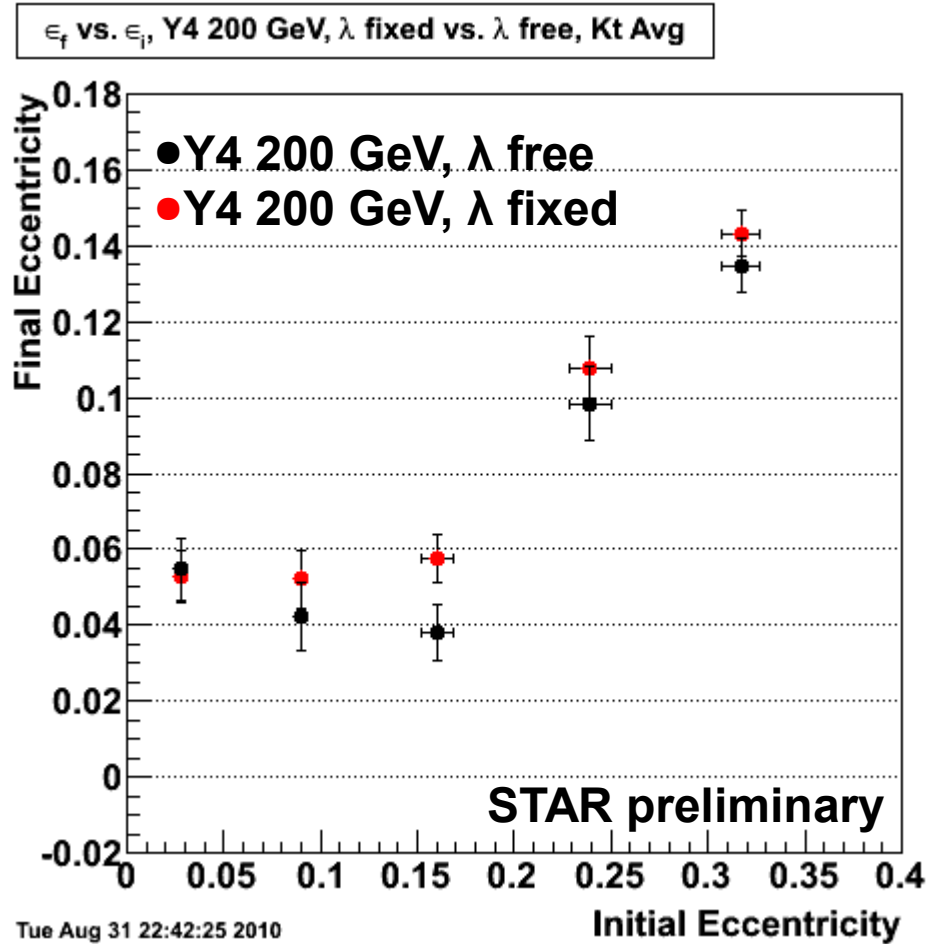
Close up of 62.4 and 200 GeV points



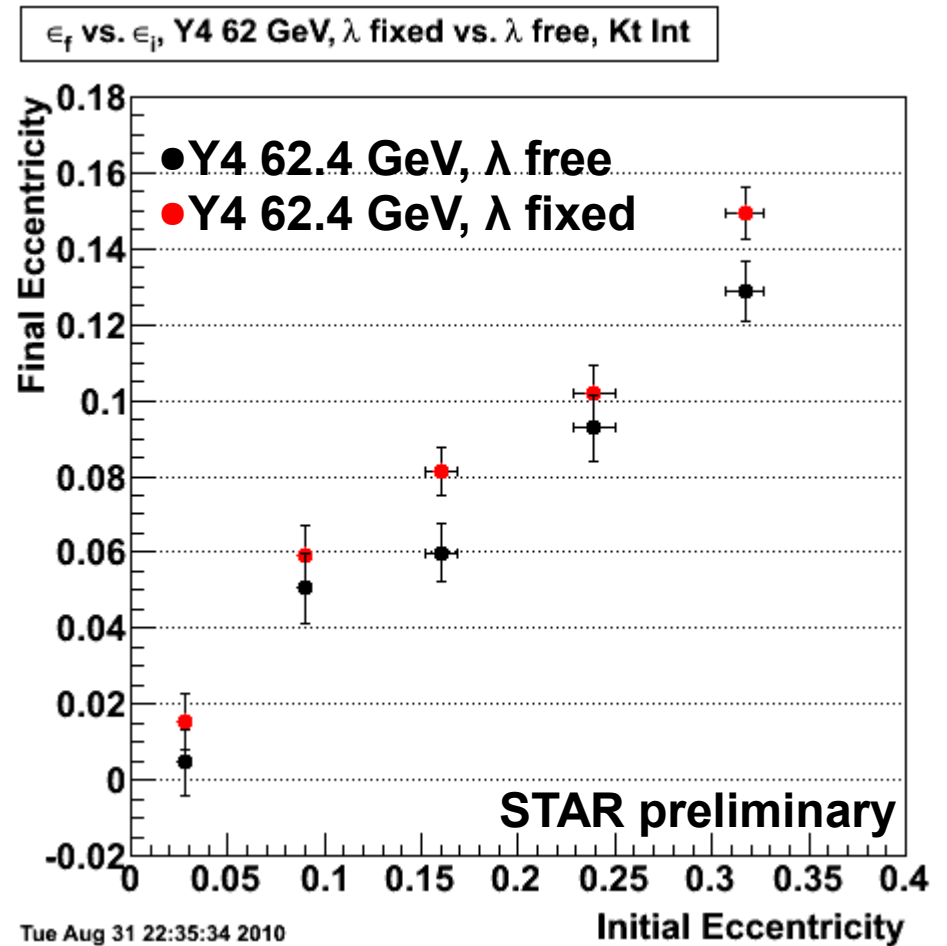
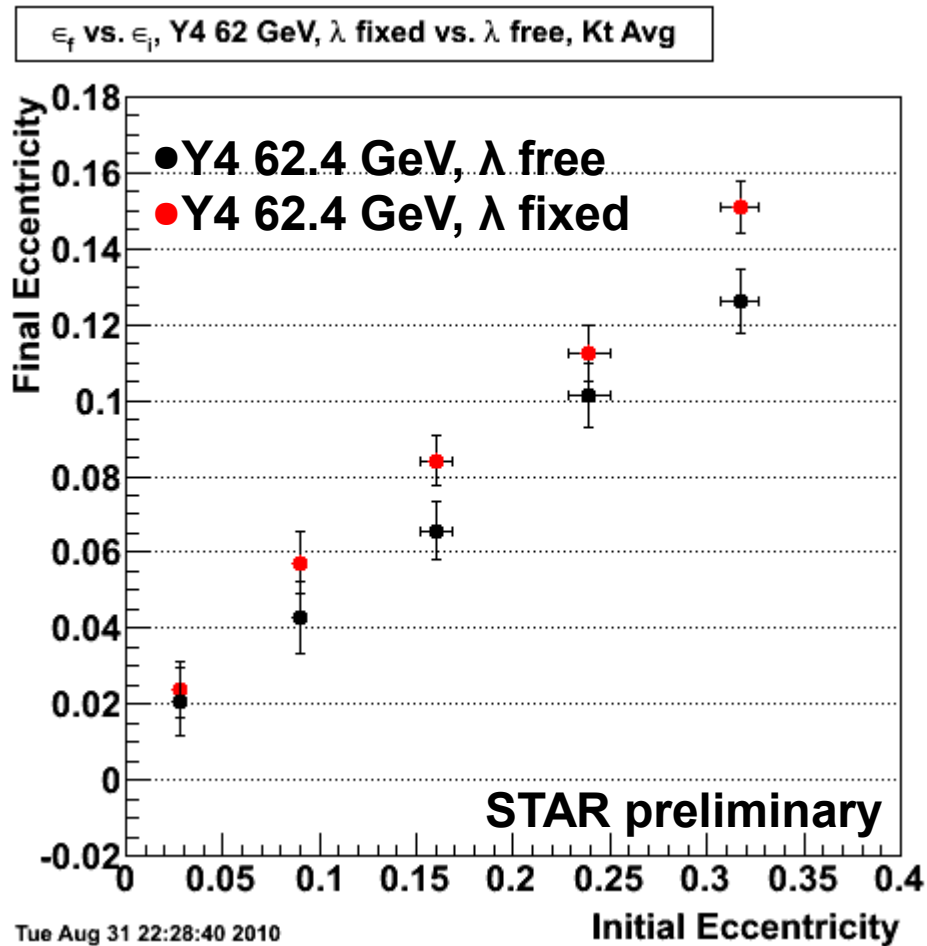
	Energy	Epsilon	EpsError
Y4 62.4 Kt Avg	62.4	0.098173750	0.009884212
Y4 62.4 Kt Int	62.4	0.091692000	0.009693387
Y4 200 Kt Avg	200	0.082621050	0.010419805
Y4 200 Kt Int	200	0.080916850	0.010353542
Y2 200 Kt Avg	200	0.094000000	0.013453624

*Points in figure are slightly offset in energy for clarity.

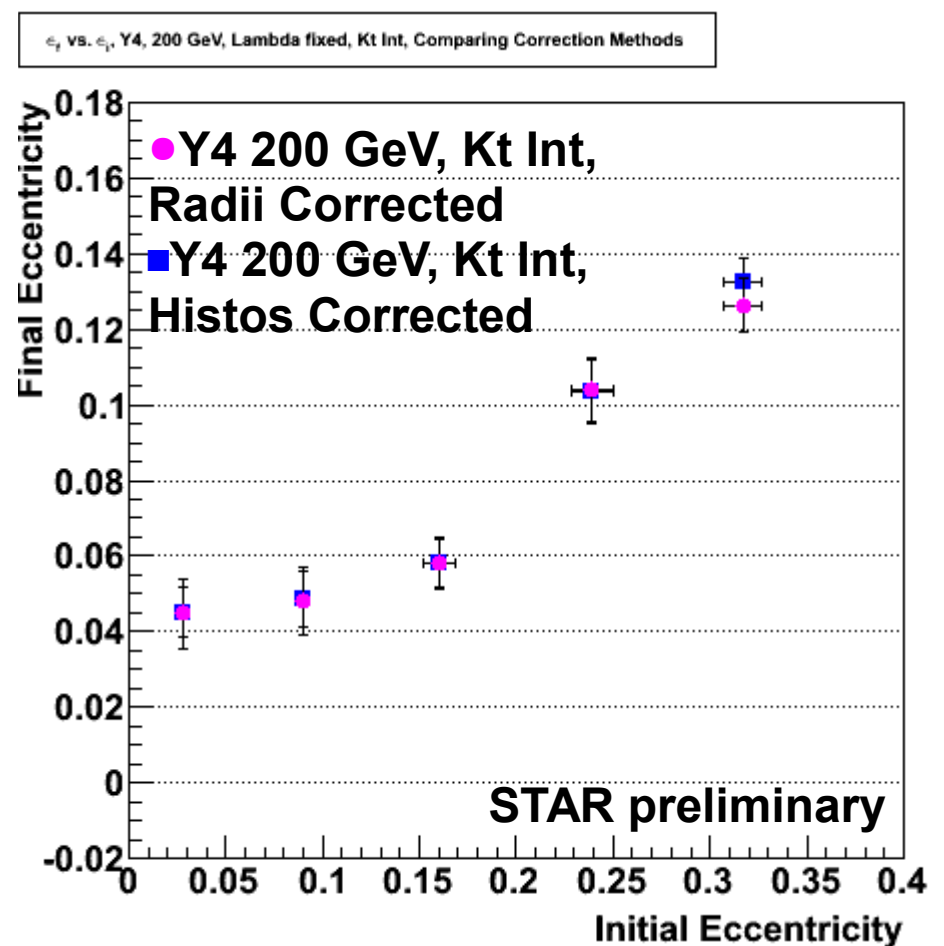
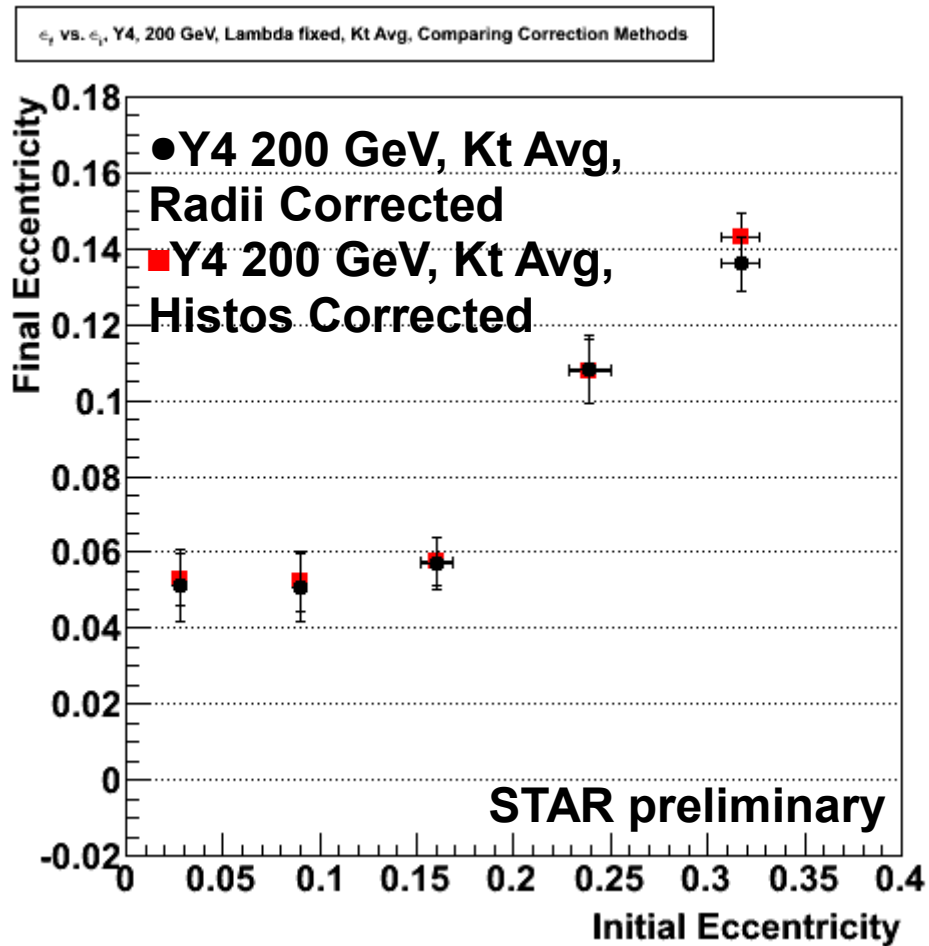
Y4 200 GeV – λ Fixed vs λ Free



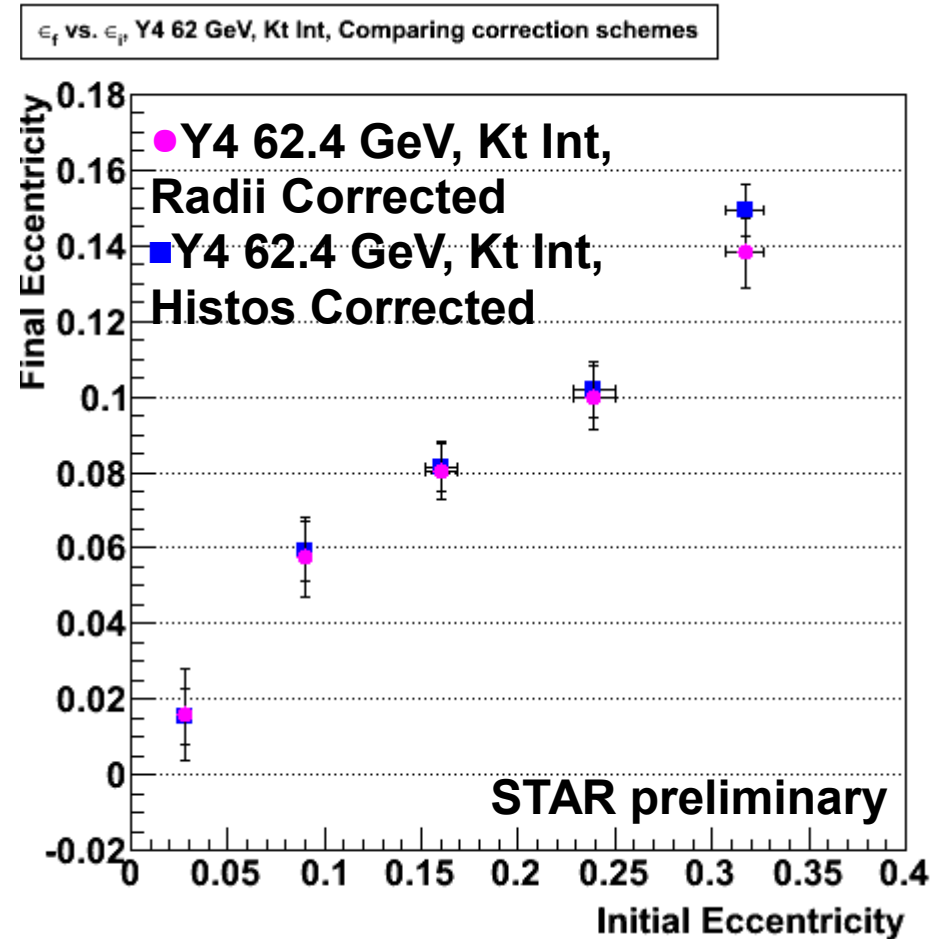
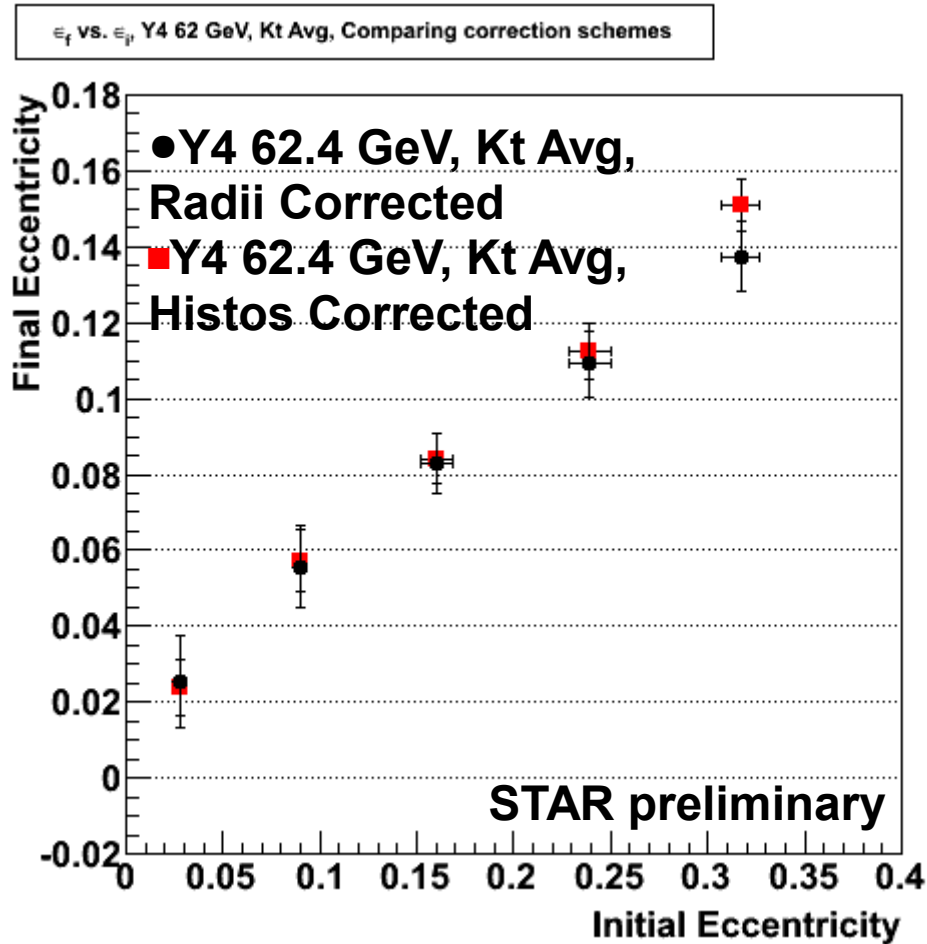
Y4 62.4 GeV – λ Fixed vs λ Free



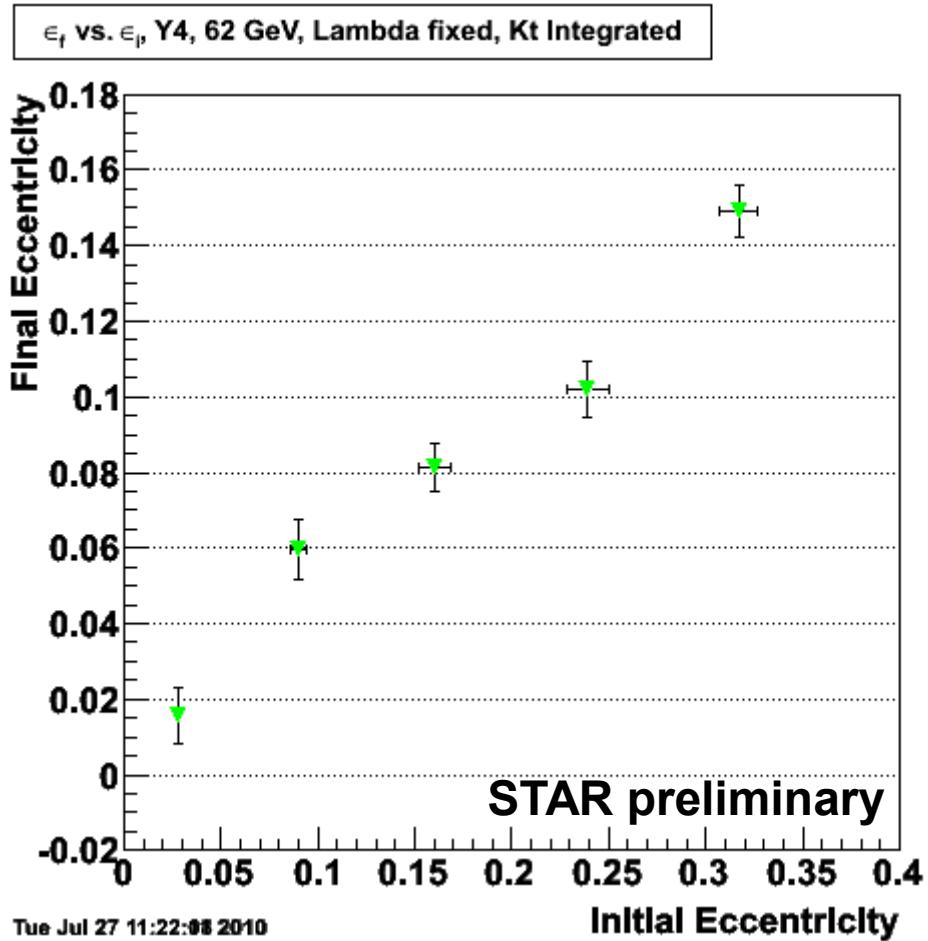
Y4 200 GeV – Two correction schemes



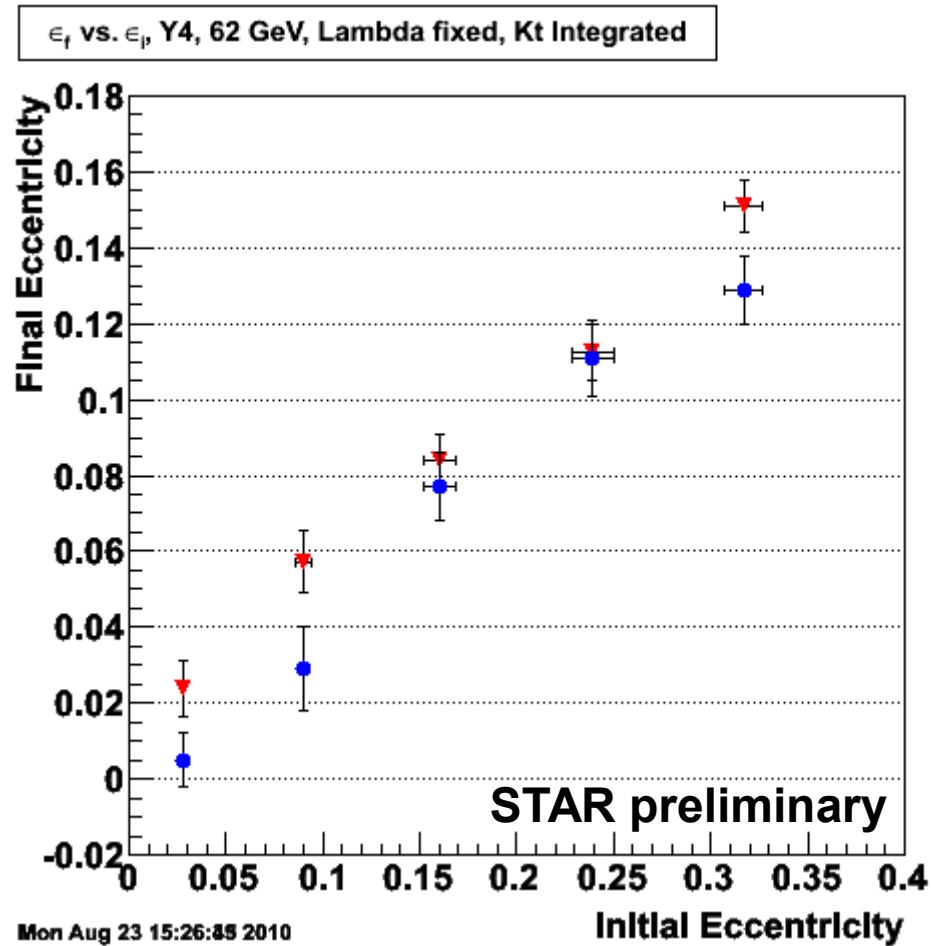
Y4 62.4 GeV – Two correction schemes



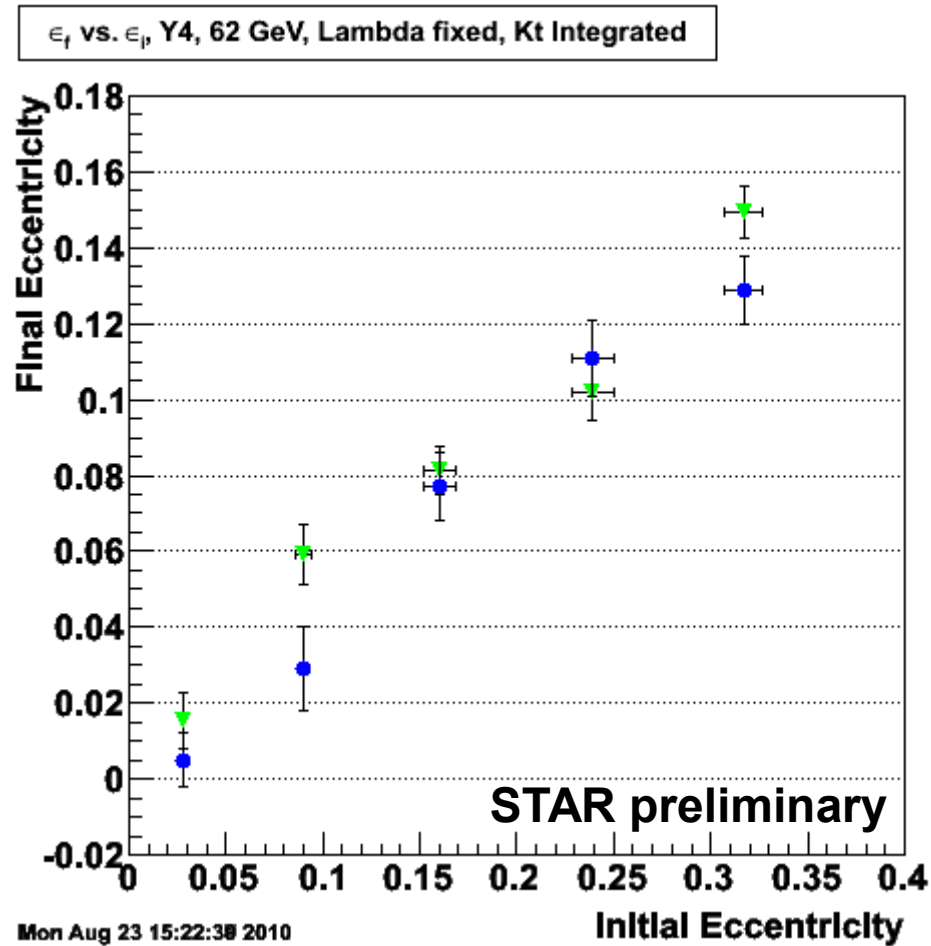
Y4 Kt Integrated at 62.4 GeV



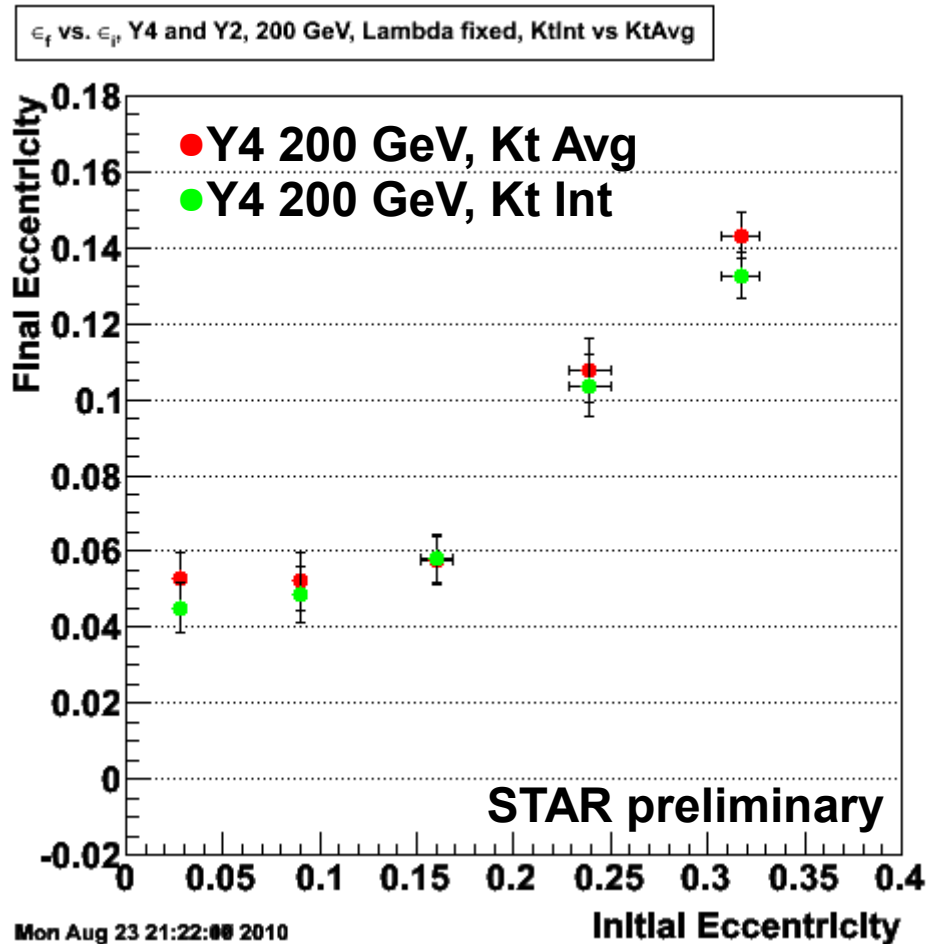
Y4 62.4 GeV vs Y2 200 GeV Kt Averaged



Y4 62.4 GeV Kt Int vs Y2 200 GeV KtAvg



Y4 Kt Averaged vs. Kt Integrated



- Kt Integrated and Kt Averaged eccentricities are similar.