

Lambda-proton femtoscopy in collisions of Ar+KCl at 1.76 AGeV with HADES

■ basics

- the correlation function (CF)
- model predictions: Λp vs. pp CF

■ exp. data (HADES)

- prerequisites: high quality Λ selection
- Λp relative-momentum CF (comparison to pp , $\pi\pi$)

■ simulation

- PLUTO \Rightarrow GEANT \Rightarrow Embedding \Rightarrow CFs of uncorrelated Λp pairs
- to correct exp. CF

■ results

- comparison to model \Rightarrow Λp source radius
- comparison to other data



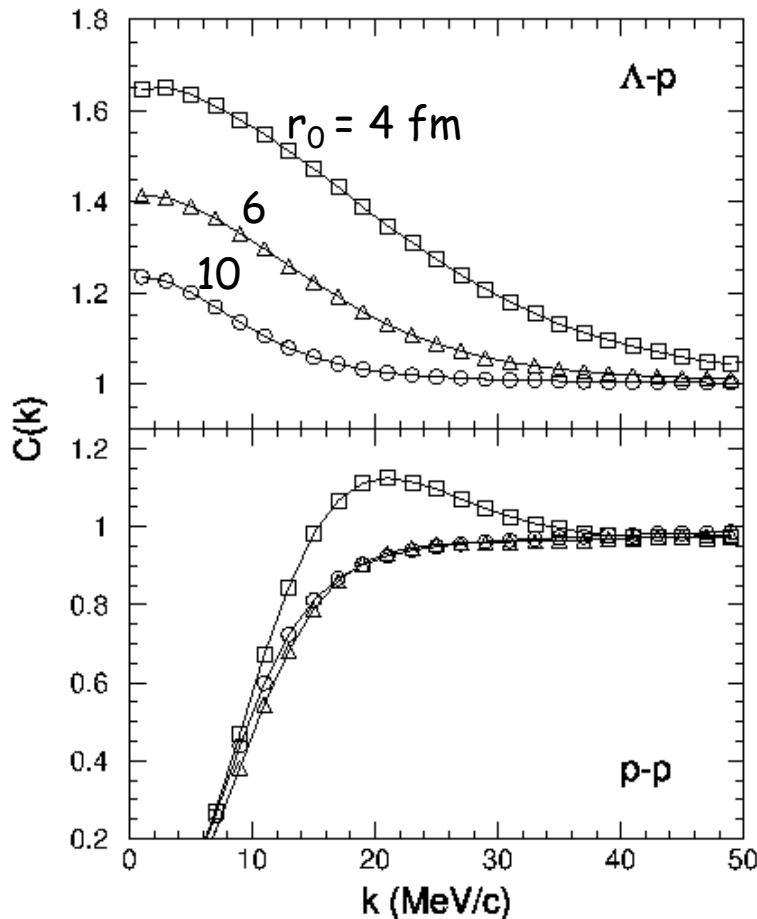
The correlation function (CF)

$$C(\mathbf{p}_1, \mathbf{p}_2) = N \frac{\sum Y_{12}(\mathbf{p}_1, \mathbf{p}_2)}{\sum Y_{12, \text{mix}}(\mathbf{p}_1, \mathbf{p}_2)}$$

- sum Σ runs over all events and pairs
- mix: take particles 1, 2 from different events
- projection on rel. momentum **in pair c.m.**
frame ($\mathbf{p}_1 + \mathbf{p}_2 = 0$): $\mathbf{k} = |\mathbf{p}_1 - \mathbf{p}_2|/2 = |\mathbf{p}|$
- normalization N: $C \Rightarrow 1$ at high k (100-150 MeV/c)



Theoretical predictions*



Λ p correlations:

- strong interaction only
(attractive Λ p potential)

r_0 : Gaussian source radius

pp correlations:

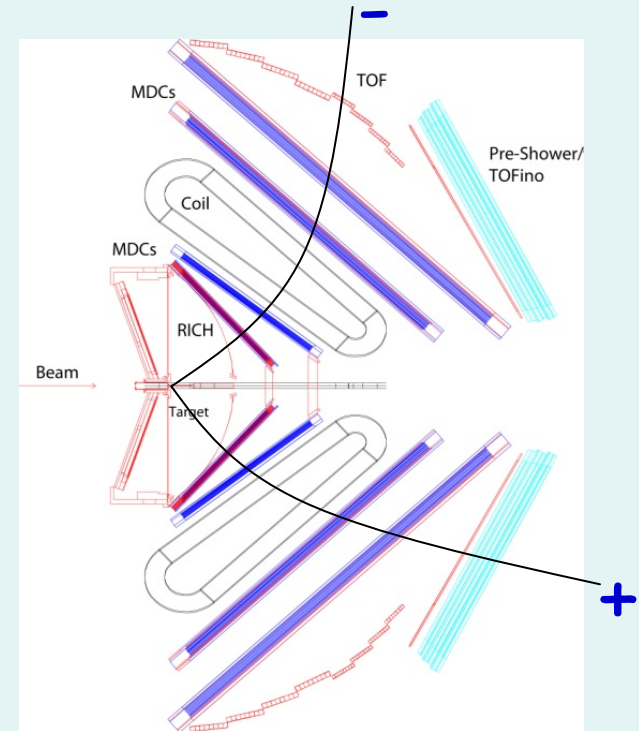
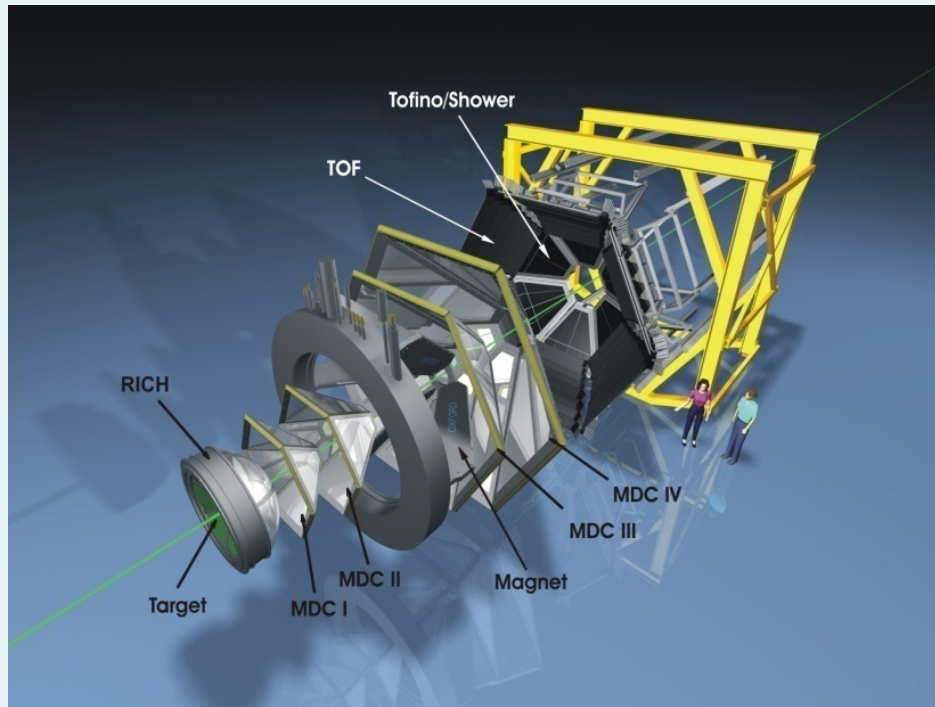
- attractive NN potential
- repulsive Coulomb potential
- suppression due to quantum (Fermi-Dirac) statistics

* F. Wang and S. Pratt, PRL 83 (1999) 3138



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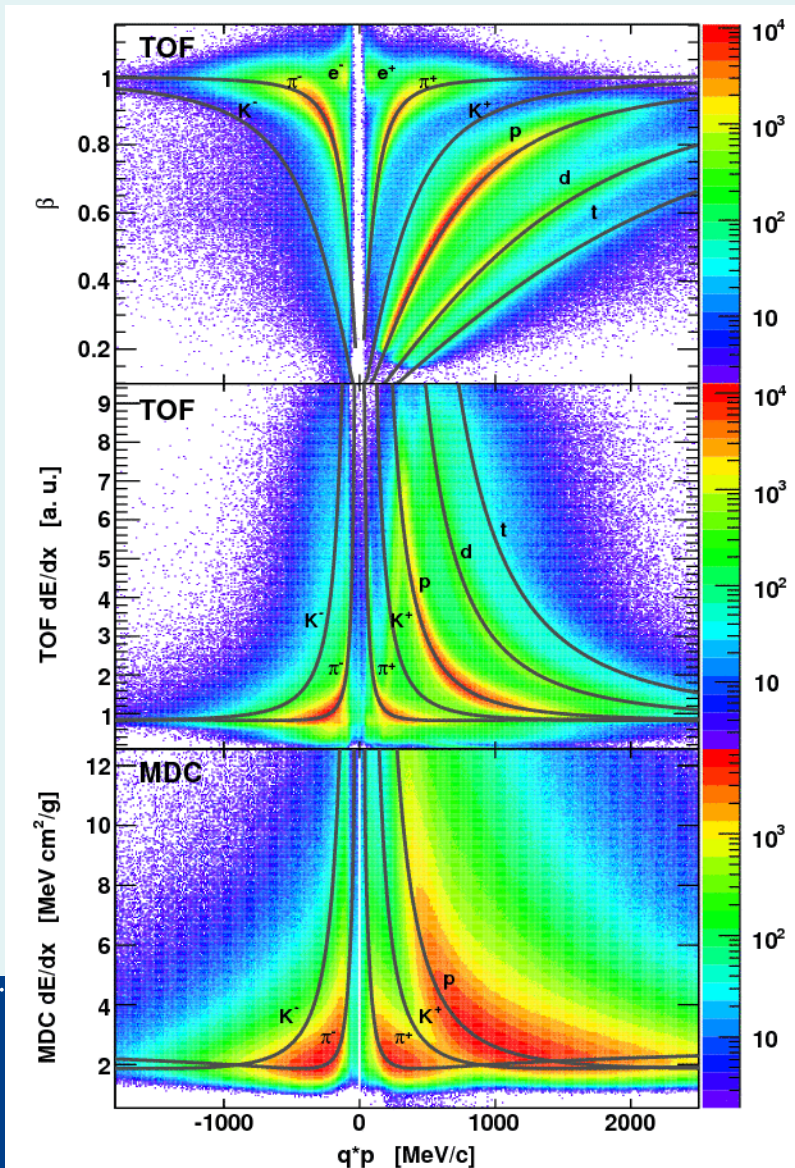
High Acceptance Di-Electron Spectrometer HADES @ SIS18, GSI Darmstadt



- high geometrical acceptance
- particle identification via dE/dx and ToF
- momentum resolution $\sim 2-5\%$



Particle ID with HADES (I)



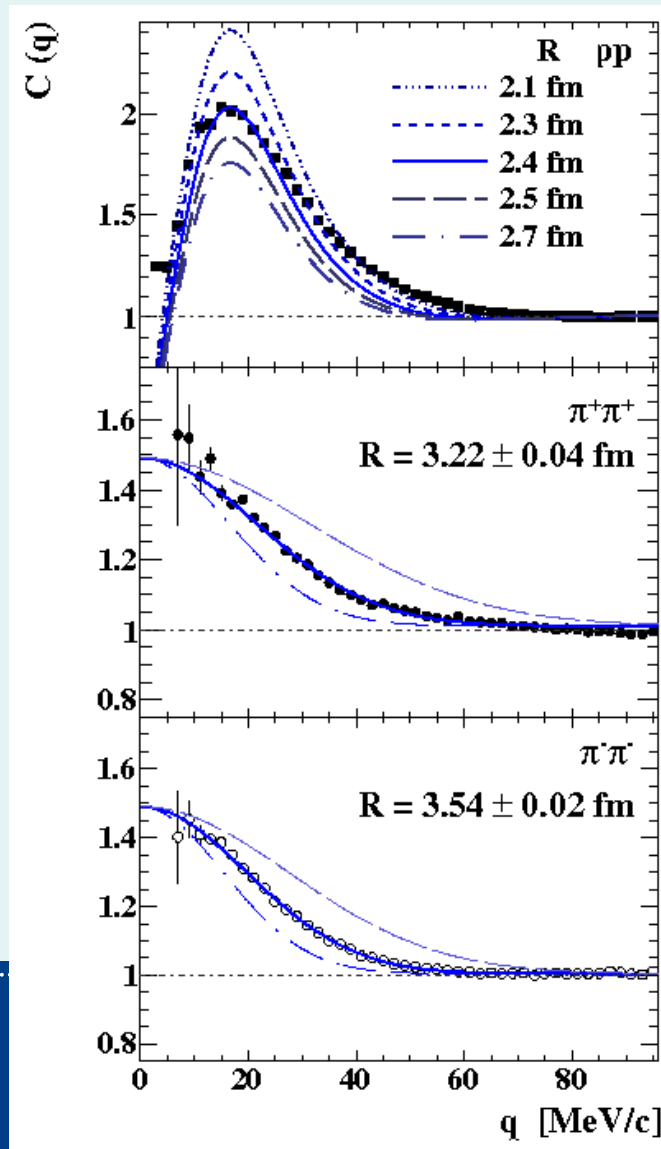
protons and
pions well
identified

pp and $\pi\pi$ correlations*

curves: Koonin model#
for various
Gaussian radii

curves: Gaussian fits
to Gamov corrected
correlation fct. and
optimum radius ± 1 fm

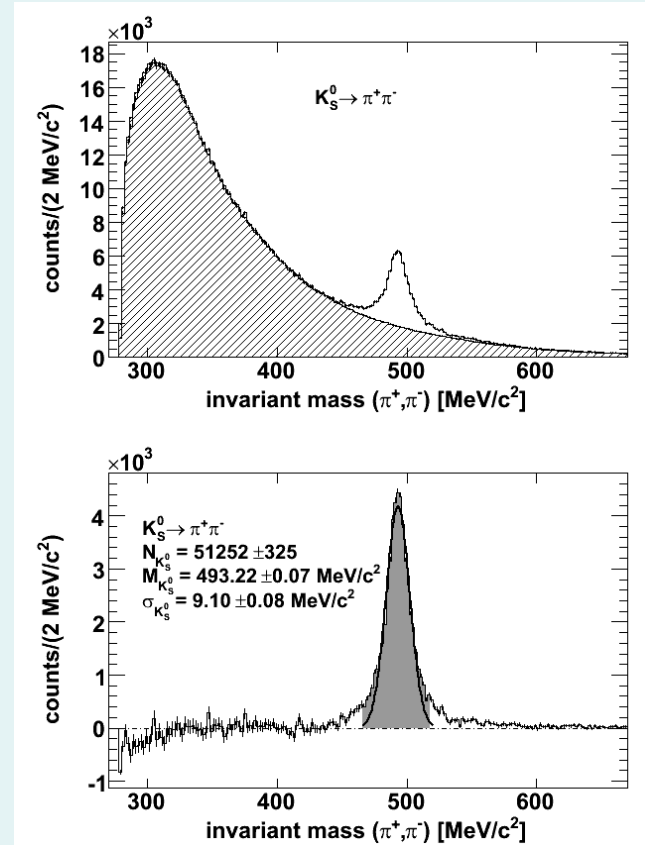
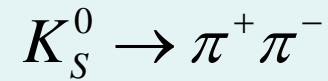
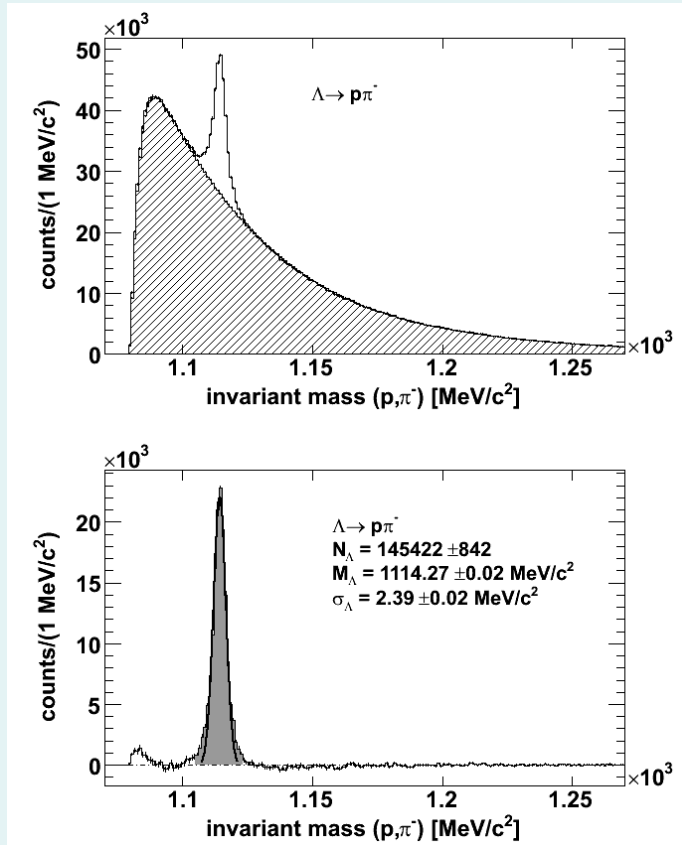
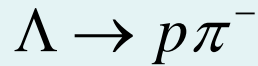
S.E. Koonin, PLB 70 (1977) 43



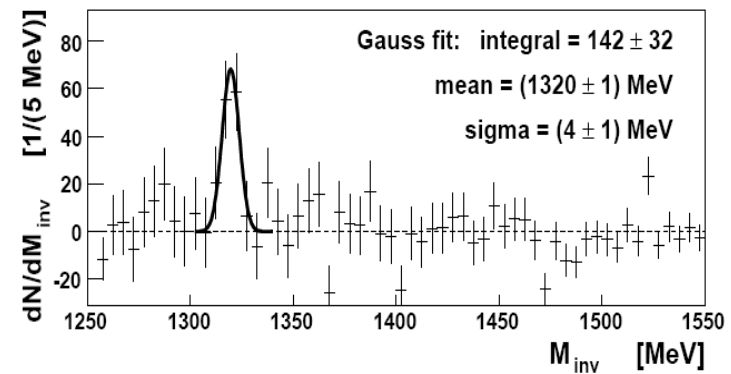
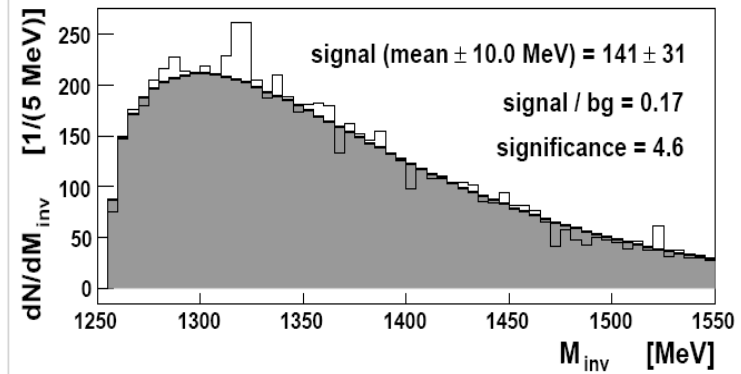
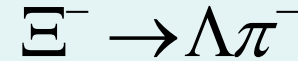
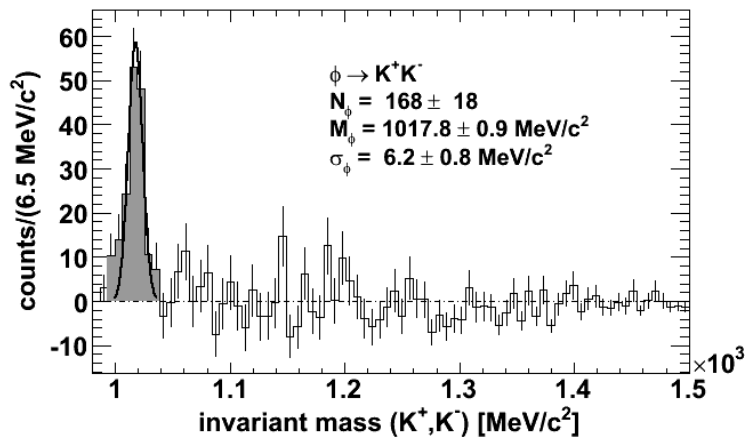
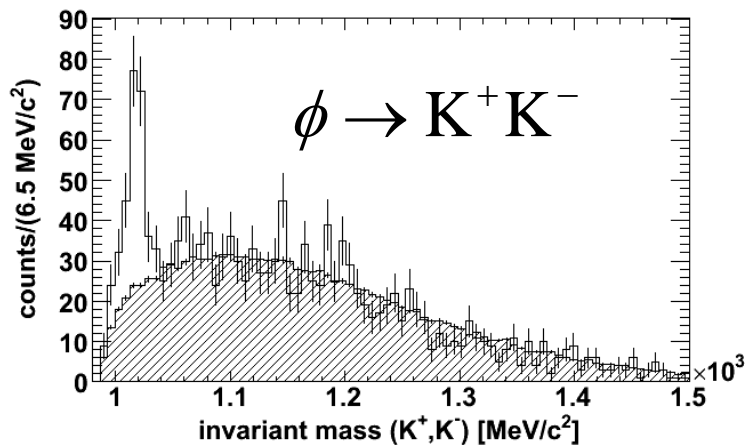
$$r_0 = (2.4 \pm 0.1^{+0.3}_{-0.1}) \text{ fm}$$

* C. Wendisch, Diploma thesis,
Techn. Univ. Dresden, 2009

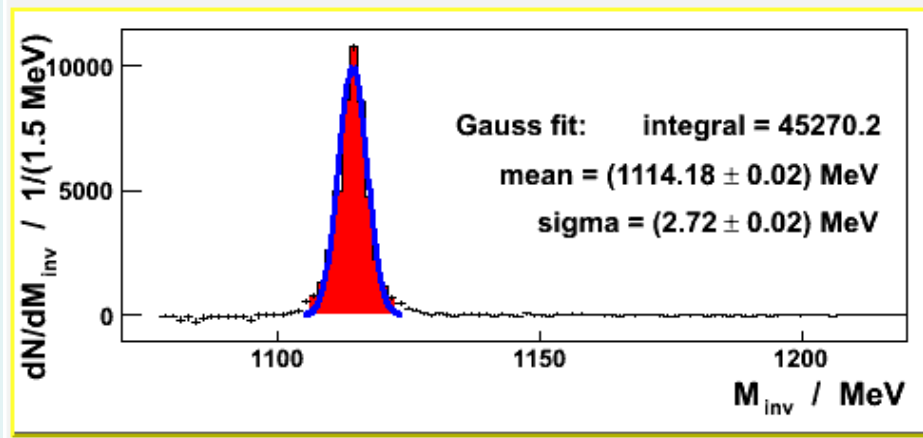
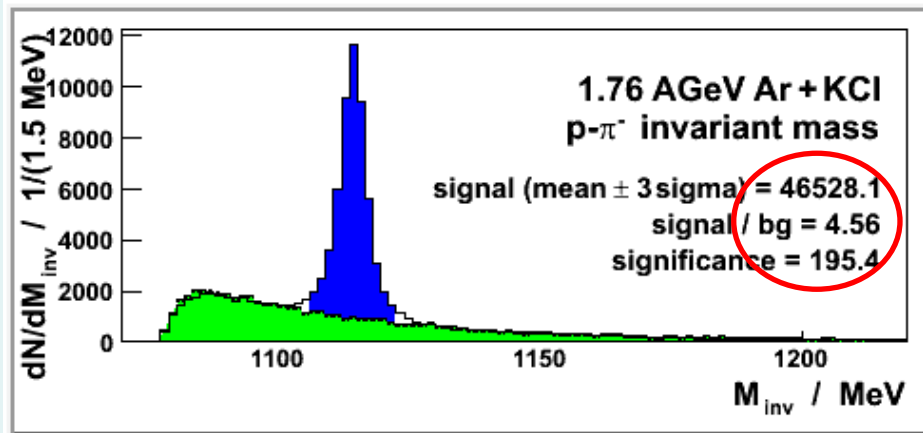
Particle ID with HADES (II)



Particle ID with HADES (III)



Prerequisite of Δp correlation study: An almost pure high-yield Λ sample



- 700 mio semi-central events (35%, $\langle b \rangle = 3.5$ fm)
- Λ cuts optimized for large signal/bg ratio

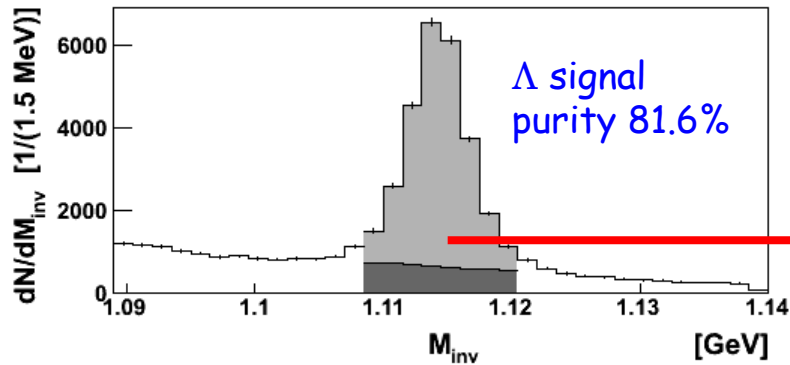
Λ yield:

$$N_{\Lambda} = 46528 \pm 566$$

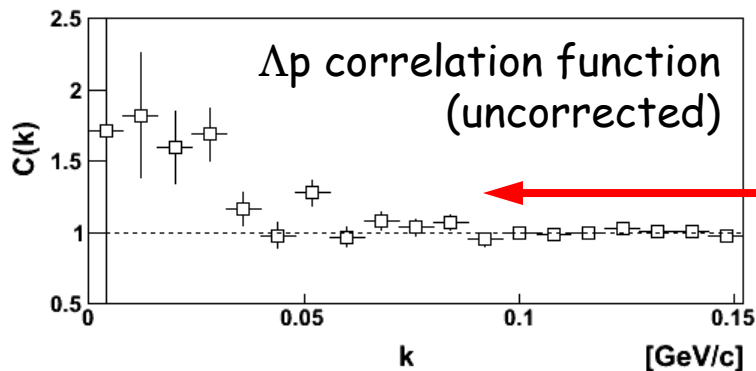
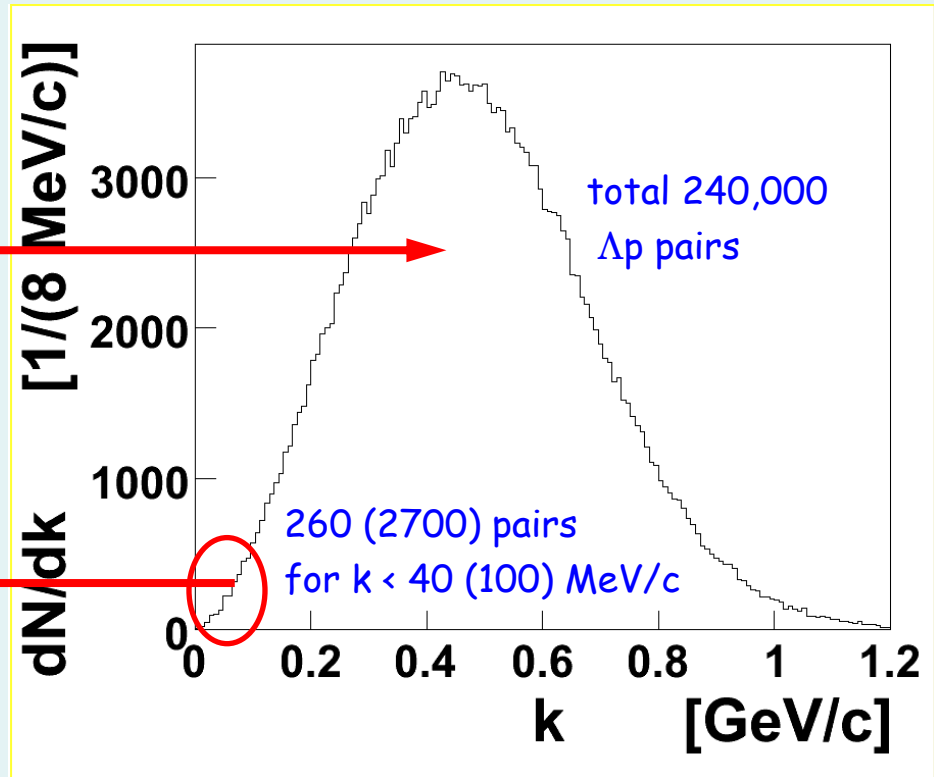


Δp correlations - Exp. Data

$p\pi^-$ invariant mass distribution



Δp relative-momentum distribution



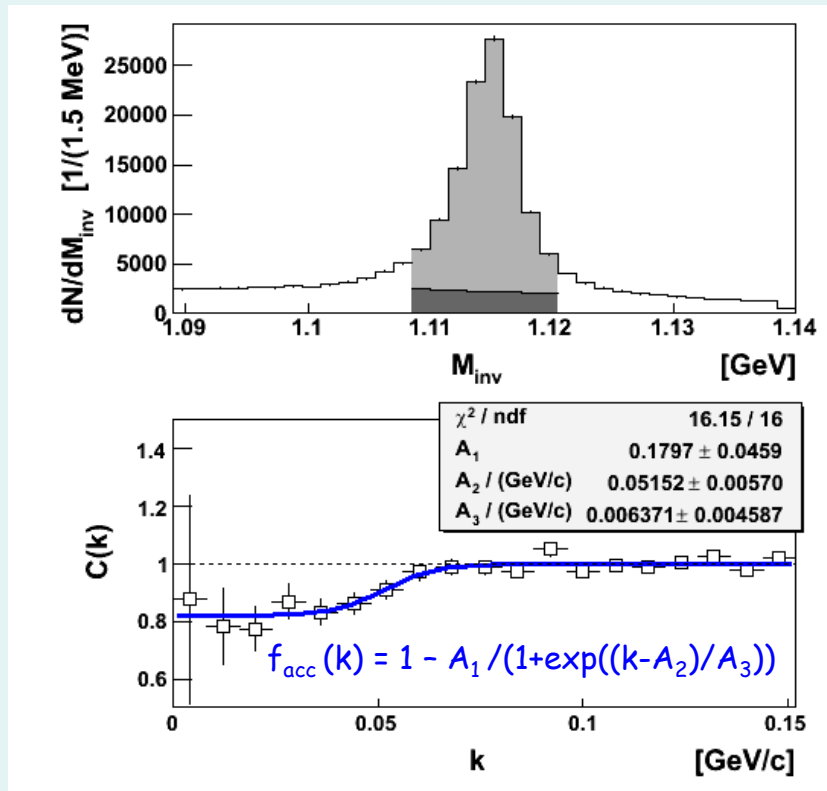
Simulations

- generate 25 million thermal Λ 's ($T=95$ MeV, $\sigma_y=0.42$) with PLUTO* event generator (1 Λ /evt)
- run GEANT (HADES detector acceptance, granularity, resolution, etc.) for PLUTO Λ 's
- embed GEANT output into exp. data
- analyse like exp. data => correlation function for uncorrelated Λp pairs (Λ : simu, p: exp)

* PoS(ACAT)076 (2007)



Λ correlations - Simulation



simulated Λ 's (decay products embedded into exp. data)

flat Λ p correlation expected:

apparent negative correlation
(due to finite near-track resolution)
used for correction of exp. CF



Corrections to the experimental Λ p correlation function

- close-track correction: $C(k) \Rightarrow C(k)/f_{acc}(k)$
fit to CF of simulated Λ 's embedded into exp. data ($A_1=0.180 \pm 0.046$)
- purity correction: $C(k) \Rightarrow 1 + (C(k)-1)/PairPurity$

$$PairPurity = LambdaPurity * ProtonPurity (0.95 \pm 0.02)$$

$$LambdaPurity = LambdaSignalPurity * PrimaryLambda$$

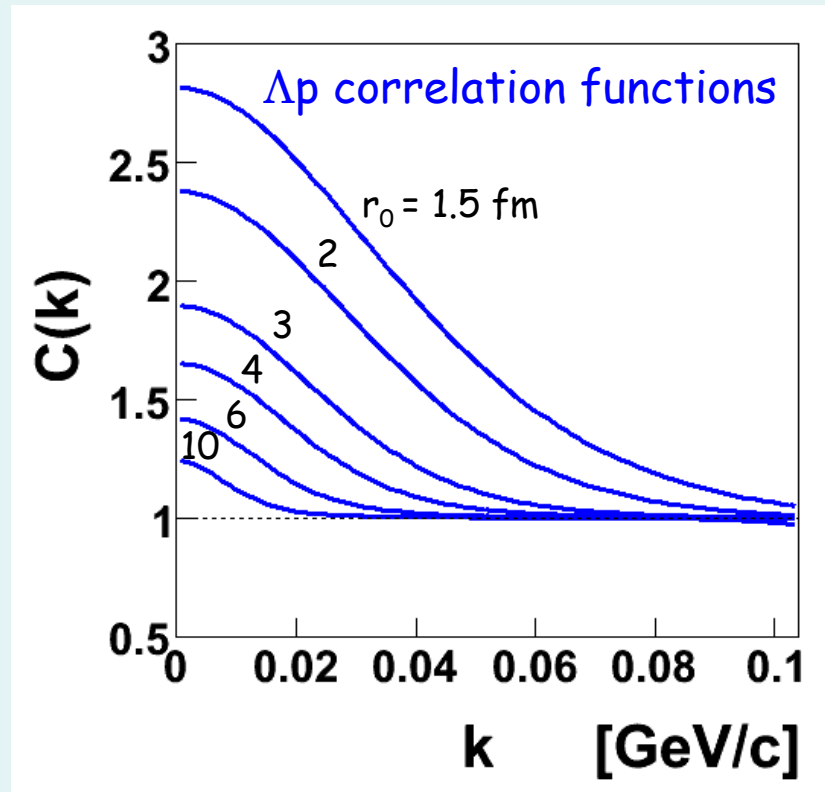
$$LambdaSignalPurity = 0.816 \pm 0.013 \quad \Leftarrow \quad p\pi^- \text{ inv. mass distr.}$$

$$PrimaryLambda = 0.90 \pm 0.10 \quad \Leftarrow \quad \begin{array}{l} 20\% \text{ feeding from } \Sigma^0 \text{ (UrQMD)} \\ 50\% \text{ loss of } \Sigma^0 p \text{ corr. after } \Sigma^0 \rightarrow \Lambda \gamma \end{array}$$



The Analytical Model by Lednicky and Lyuboshitz[#]

Variation
of Gaussian
source radius:



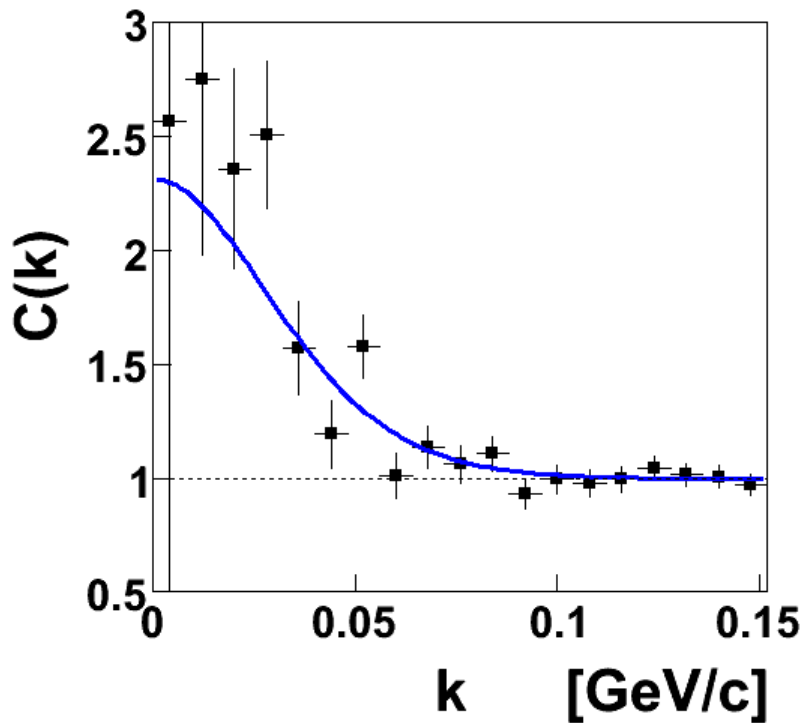
r_0 : the only free
parameter

=> radius affects
both height AND
width of CF

[#] R. Lednicky, V.L. Lyuboshitz, Sov. J. Nucl. Phys. 35 (1982) 770; see: J. Adams et al. (STAR), PRC 74 (2006) 064906



Close-track resolution and purity corrected Δp correlation function - Fit with Lednicky Analytical Model



maximum likelihood* =>

$$r_0 = (2.09 \pm 0.16 \begin{matrix} +0.12 & +0.09 & +0.09 \\ -0.10 & -0.16 & -0.11 \end{matrix}) \text{ fm}$$

syst. errors:

#1: uncertainty of close-track correction

#2: uncertainty of purity correction

#3: variation of scattering lengths (in model) by $\pm 25\%$

* L. Ahle et al. (E802), PRC 66 (2002) 054906



Varying the whole set of scattering lengths and effective ranges + Fit with Lednicky Analytical Model

parameter / data set	singlet		triplet		r_0 [fm]
	f_0^s [fm]	d_0^s [fm]	f_0^t [fm]	d_0^t [fm]	
EFT '06 [1]	-1.91	1.39	-1.23	2.16	2.13±0.15
Jülich '04 [1]	-2.56	2.75	-1.66	2.93	2.15±0.15
Nijmegen NSC97f [1]	-2.51	3.03	-1.75	3.32	2.11±0.15
Wang & Pratt [2]	-2.88	2.92	-1.66	3.78	2.09±0.16

quite similar source radii \Rightarrow Δp correlation function hardly sensitive to specifics of Δp potential



results of maximum likelihood fit

[1] J. Haidenbauer et al., Lect. Notes Phys. 724 (2007) 113

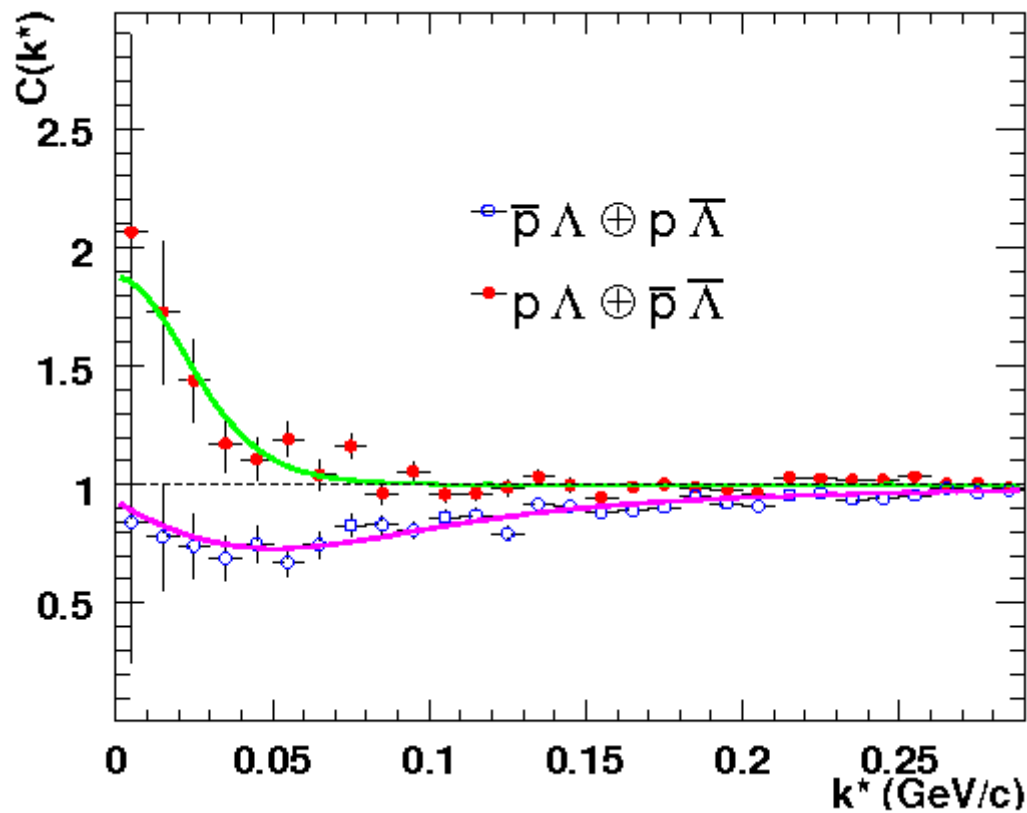
[2] F. Wang and S. Pratt, PRL 83 (1999) 3138



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Comparison with RHIC data*

Central (10%) Au+Au @ $\sqrt{s_{NN}} = 200 \text{ GeV}$



Lines: fits with Analytical Model by Lednicky and Lyuboshitz[#]

$r_0 = (3.1 \pm 0.3 \pm 0.2) \text{ fm}$

($k^* = |\mathbf{p}_1 - \mathbf{p}_2|/2$ in pair c.m. frame)

[#] R. Lednicky and V.L. Lyuboshitz, Sov. J. Nucl. Phys. 35 (1982) 770

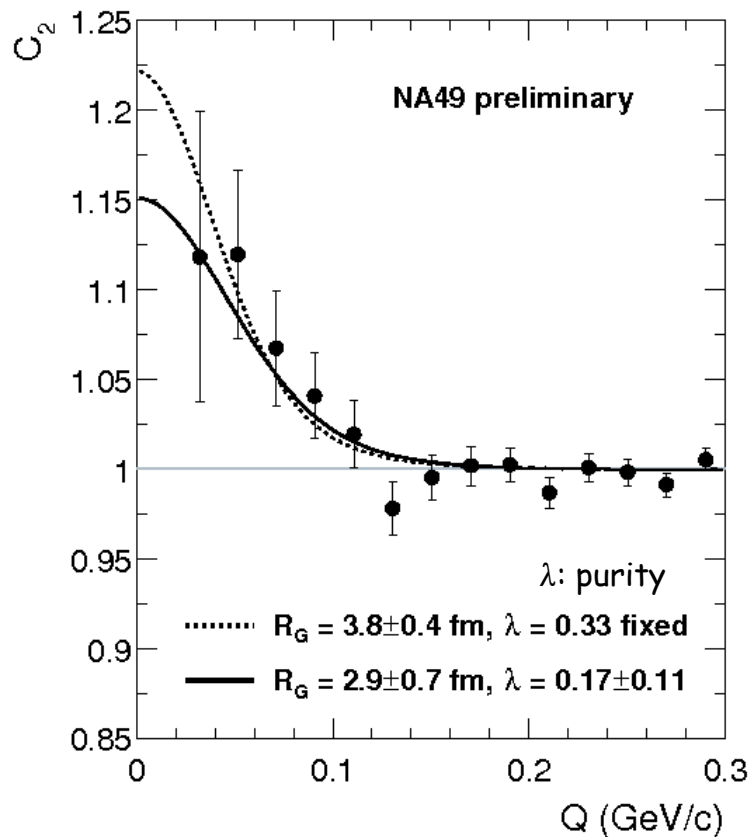
* J. Adams et al. (STAR), PRC 74 (2006) 064906



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Comparison with SPS data*

Central (10%) Pb+Pb @ 158 AGeV



Lines: fits with Analytical Model by Lednicky and Lyuboshitz#

$$r_0 = 3 - 4 \text{ fm}$$

($Q = |\mathbf{p}_1 - \mathbf{p}_2|$ in pair c.m. frame)

R. Lednicky and V.L. Lyuboshitz, Sov. J. Nucl. Phys. 35 (1982) 77

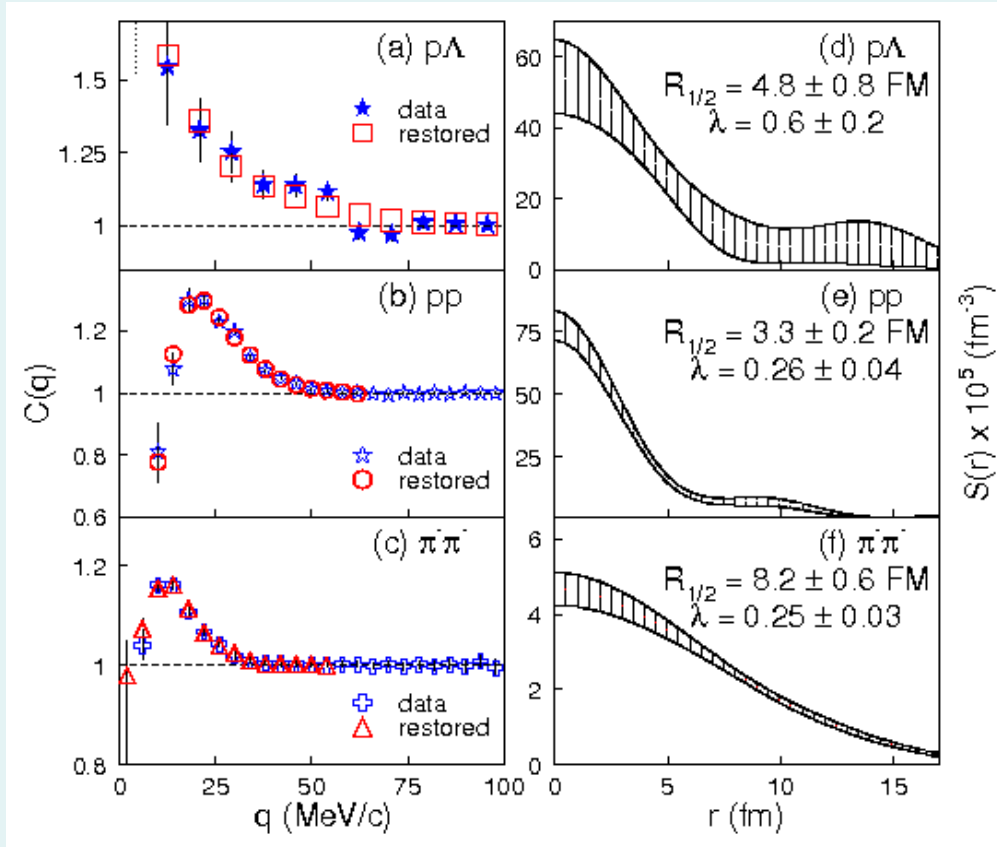
* C. Blume et al. (NA49), Proc. Quark Matter 2002, Nantes, France, NPA 715 (2003) 55c



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Comparison with AGS data*

Semi-central (23%) Au+Au @ 6 AGeV



left: correlation functions (CFs)

right: imaged sources by numerical inversion of CF

$R_{1/2}$: half-maximum radius

$$\Rightarrow r_0(p\Lambda) = (4.1 \pm 0.7) \text{ fm}$$

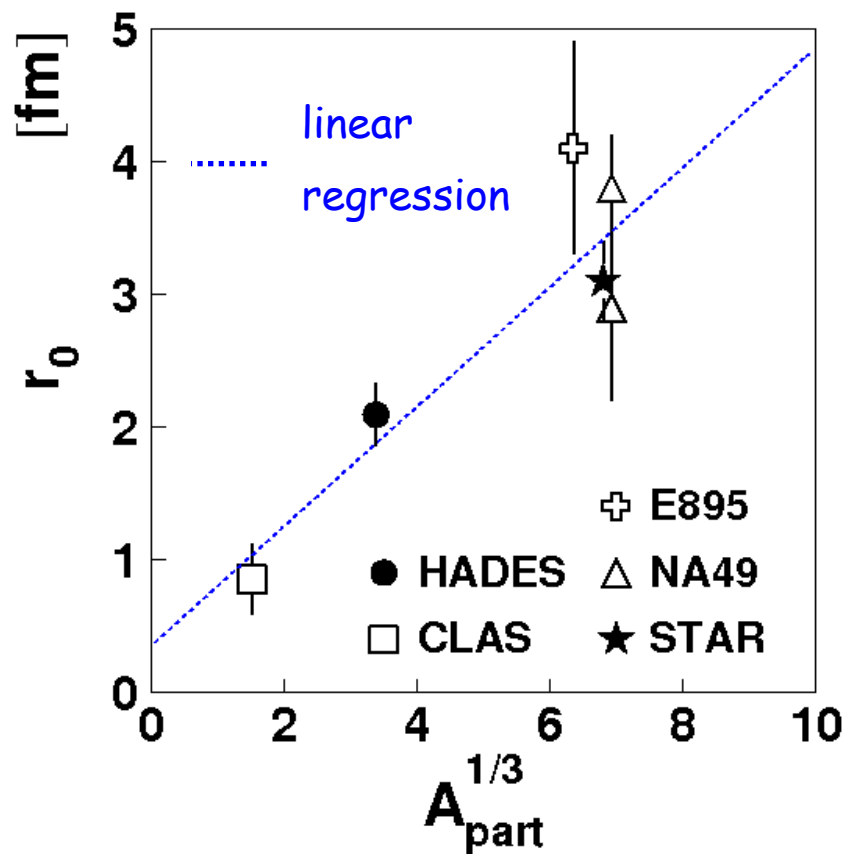
($q = |\mathbf{p}_1 - \mathbf{p}_2|/2$ in pair c.m. frame)

* P. Chung et al. (E895),
PRL 91 (2003) 162301



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System-size dependence of Λ_p source radius



- E895: Au+Au [PRL 91 (2003) 162301]
- NA49: Pb+Pb [NPA 715 (2003) 55c]
- STAR: Au+Au [PRC 74 (2005) 064906]
- CLAS: $e+^{3,4}\text{He}$ [Phys. Atom. Nucl. 72 (2009) 668]
- HADES: Ar+KCl (note the precision!)

=> almost linear increase



Summary

- first time at SIS energies (Ar+KCl @ 1.76 AGeV):
 Λ p correlations*

- prerequisite: high-yield and high-purity Λ sample

- comparison to model by Lednicky & Lyuboshitz

=> Gaussian radius of Λ p emission source

$$r_0 = (2.09 \pm 0.16^{+0.17}_{-0.22}) \text{ fm}$$

- Λ p correlation function hardly sensitive to specifics of Λ p potential

- r_0 slightly smaller than pp correlation radius

- Λ p radius in Ar+KCl smaller than in Au+Au/Pb+Pb but

larger than in e+He => linear increase of r_0 with $A_{\text{part}}^{1/3}$

* G. Agakishiev et al., PRC 82 (2010) 021901



The HADES collaboration

Catania (INFN - LNS), Italy
Coimbra (Univ.), LIP, Portugal
Cracow (Univ.), Poland
Darmstadt (GSI), Germany
Dresden (FZD), Germany
Dubna (JINR), Russia
Frankfurt (Univ.), Germany
Giessen (Univ.), Germany

Milano (INFN, Univ.), Italy
Moscow (ITEP, MEPhI, RAS), Russia
Munich (TUM), Germany
Nicosia (Univ.), Cyprus
Orsay (IPN), France
Rez (CAS, NPI), Czech Rep.
Sant. de Compostela (Univ.), Spain
Valencia (Univ.), Spain

